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NATIONAL SENIOR CERTIFICATE

GRADE 12

MATHEMATICS

COMMON TEST

MARCH 2025

MARKS: 100

TIME: 2 hours

N.B. This question paper consists of 7 pages and an information sheet.



INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of 6 questions.
2. Answer **ALL** questions.
3. Clearly show **ALL** calculations, diagrams, graphs, et cetera that you have used in determining your answers.
4. Answers only will not necessarily be awarded full marks.
5. An approved scientific calculator (non-programmable and non-graphical) may be used, unless stated otherwise.
6. If necessary, answers should be rounded off to **TWO** decimal places, unless stated otherwise.
7. Diagrams are **NOT** necessarily drawn to scale.
8. Number the answers correctly according to the numbering system used in this question paper. Write neatly and legibly.



QUESTION 1

- 1.1 Given: The sum to n terms of an arithmetic sequence is $S_n = 3n^2 - 5n$.
- 1.1.1 Calculate the sum of the first 21 terms of this sequence. (2)
- 1.1.2 Determine the 22nd term of this sequence. (2)
- 1.1.3 How many terms of this sequence must be added to obtain a sum of 8162? (4)
- 1.2 Consider the sequence: 7 ; 7 ; 7 ; 12 ; 7 ; 17 ; 7 ; 22; ...
- 1.2.1 Determine the value of the 78th term of this sequence. (2)
- 1.2.2 Calculate the sum of the first 103 terms of this sequence. (4)
- [14]**

QUESTION 2

- 2.1 Given: $\sum_{k=2}^{13} (-3)^k$
- 2.1.1 Write down the values of the first three terms of the series. (2)
- 2.1.2 Write down the value of the constant ratio. (1)
- 2.1.3 Will $\sum_{k=2}^{\infty} (-3)^k$ converge? Explain your answer. (2)
- 2.1.4 Calculate $\sum_{k=2}^{13} (-3)^k x$. Give your answer in terms of x . (3)
- 2.2 A quadratic sequence with a general term T_n has the following properties:
- $T_{29} = 1166$
 - $T_n - T_{n-1} = 3n - 4$
- Determine the value of the first term of the quadratic sequence. (6)
- [14]**



QUESTION 3

3.1 Given: $f(x) = \frac{2x+3}{-x-3}$

3.1.1 Show that $f(x)$ can also be written as $f(x) = \frac{3}{x+3} - 2$. (2)

3.1.2 Hence, determine the coordinates of the intercepts of f with the axes. (3)

3.1.3 Sketch the graph of f . Clearly indicate the intercepts with both axes, as well as the asymptotes. (3)

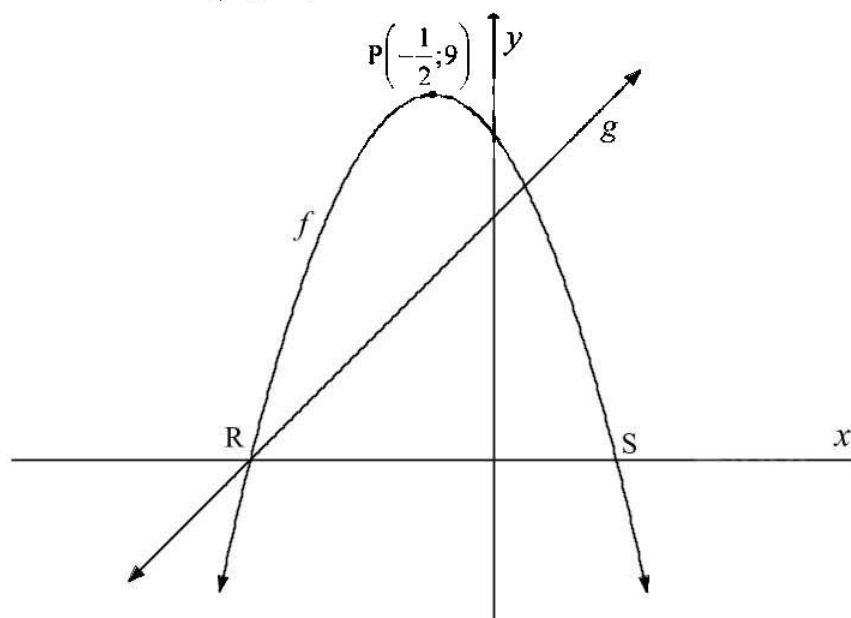
3.1.4 Determine the equation of the axis of symmetry of f , which is a decreasing function. (2)

3.1.5 Determine the value(s) of x for which:

(a) f is decreasing. (2)

(b) $f(x) \geq 0$. (2)

3.2 Sketched below is the parabola f and the straight line $g(x) = 3x + 6$. R and S are the x -intercepts of f , and $P\left(-\frac{1}{2}; 9\right)$ is its turning point. g has its x -intercept at R.



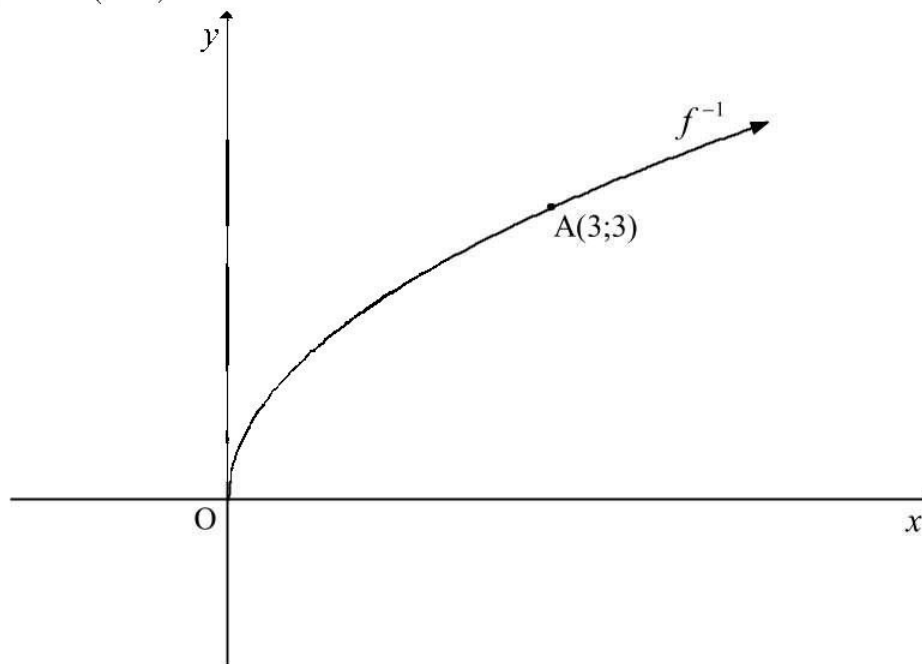
3.2.1 Calculate the coordinates of R. (2)

3.2.2 Determine the equation of the parabola. (4)

[20]

QUESTION 4

- 4.1 The graph of $f^{-1}(x) = \sqrt{3x}$, $x \geq 0$ is drawn in the sketch below. f^{-1} passes through the point $A(3; 3)$.



- 4.1.1 Determine the equation of f in the form $y = \dots\dots\dots$ (3)
- 4.1.2 For which values of x will $f(x) \leq f^{-1}(x)$? (2)
- 4.2 Consider $g(x) = \left(\frac{1}{3}\right)^x$.
- 4.2.1 Determine the equation of g^{-1} in the form $y = \dots\dots\dots$ (2)
- 4.2.2 Draw a sketch graph of g^{-1} , indicating any intercepts with the axes as well as one more point on the graph. (3)
- 4.2.3 The graph of $h(x) = a\left(\frac{1}{3}\right)^x + 7$ passes through the point $(-2; 10)$. Calculate the value of a . (2)
- 4.2.4 Describe the translation from h to g . (3)

[15]



QUESTION 5

5.1 If $5 \sin \beta - 4 = 0$ and $\beta \in (90^\circ ; 270^\circ)$, determine without the use of a calculator and with the aid of a diagram the values of:

5.1.1 $\cos \beta$ (3)

5.1.2 $\cos 2\beta$ (3)

5.1.3 $\sin 3\beta$ (4)

5.2 Simplify:

$$\frac{\sin(-180^\circ - \theta) \cdot \tan(180^\circ - \theta) \cdot \cos(-\theta)}{\cos^2(90^\circ + \theta) + 3\sin^2 \theta} \quad (6)$$

5.3 Prove the identity:

$$\frac{1}{8}(1 - \cos 4x) = \sin^2 x \cdot \cos^2 x \quad (5)$$

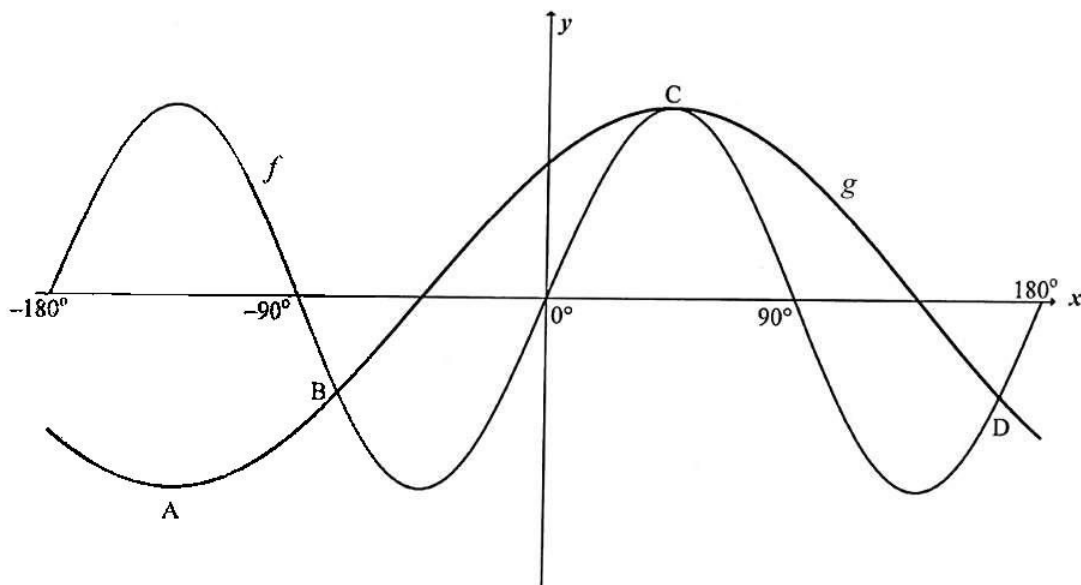
[21]



QUESTION 6

6.1 Determine the general solution of $\cos(x - 45^\circ) = \sin 2x$. (4)

6.2 In the diagram, the graphs of $f(x) = \sin 2x$ and $g(x) = \cos(x - 45^\circ)$ are drawn for the interval $x \in [-180^\circ; 180^\circ]$. A is a minimum point on graph g , and C is a maximum point on both graphs. The two graphs intersect at B, C and D.



6.2.1 Write down the period of g . (1)

6.2.2 Write down the coordinates of

(a) A (2)

(b) B (2)

6.2.3 Use the graphs to determine the values of x in the interval $x \in [0^\circ; 180^\circ]$ for which $\frac{f(x)}{g(x)} < 0$. (2)

6.2.4 Solve for x in the interval $x \in [0^\circ; 180^\circ]$ if $\sin 2x \geq \frac{1}{\sqrt{2}}(\cos x + \sin x)$. Show all your working. (5)

[16]

TOTAL: 100 marks



INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n - 1)d$$

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; -1 < r < 1$$

$$F = \frac{x[(1 + i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1 + i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \triangle ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{area } \triangle ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cdot \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

