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VHEMBE WEST DISTRICT

GRADE 12

MATHEMATICS P2

PRE-MIDYEAR EXAMINATION 2024

MEMORANDUM

MARKS: 140

This question paper consists of 21 pages including the cover page



NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

NOTA:

- *As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.*
- *As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.*
- *Volg Houe akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.*
- *Om antwoorde/waardes te aanvaar om 'n probleem op te los, word NIE toegelaat NIE.*

GEOMETRY • MEETKUNDE	
S	A mark for a correct statement (A statement mark is independent of a reason)
	<i>'n Punt vir 'n korrekte bewering ('n Punt vir 'n bewering is onafhanklik van die rede)</i>
R	A mark for the correct reason (A reason mark may only be awarded if the statement is correct)
	<i>'n Punt vir 'n korrekte rede ('n Punt word slegs vir die rede toegeken as die bewering korrek is)</i>
S/R	Award a mark if statement AND reason are both correct
	<i>Ken 'n punt toe as die bewering EN rede beide korrek is</i>



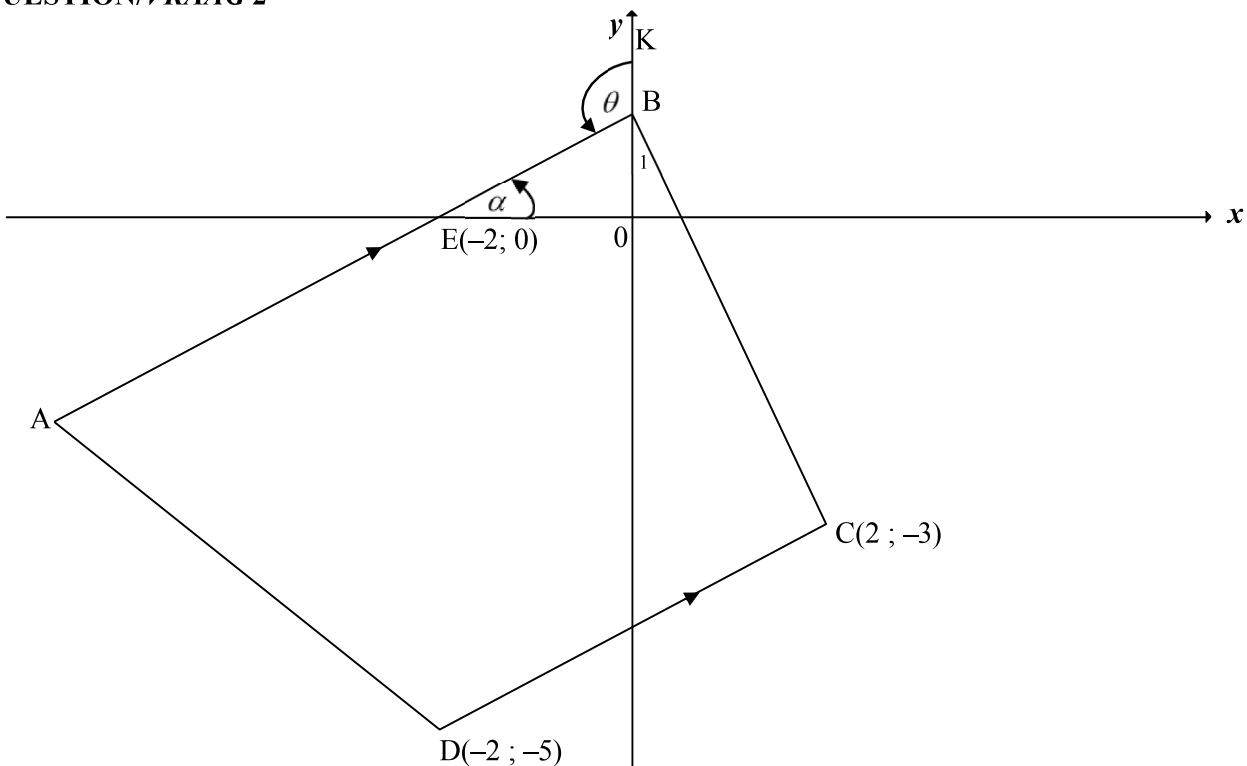
QUESTION/VRAAG 1

1.1	45 children	✓ answer (1)																								
1.2	$\bar{x} = \frac{\sum fx}{x} = \frac{(4 \times 2) + (8 \times 10) + (12 \times 9) + (16 \times 7) + (20 \times 8) + (24 \times 7) + (28 \times 2)}{45}$ $x = \frac{692}{45} \text{ OR } x = 15,38 \text{ minutes}$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: full marks</div>	✓ 692 ✓ answer (2)																								
1.3	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th>Time taken (<i>t</i>) (in minutes)</th> <th>Number of children</th> <th>Cumulative frequency</th> </tr> </thead> <tbody> <tr> <td>$2 < t \leq 6$</td> <td>2</td> <td>2</td> </tr> <tr> <td>$6 < t \leq 10$</td> <td>10</td> <td>12</td> </tr> <tr> <td>$10 < t \leq 14$</td> <td>9</td> <td>21</td> </tr> <tr> <td>$14 < t \leq 18$</td> <td>7</td> <td>28</td> </tr> <tr> <td>$18 < t \leq 22$</td> <td>8</td> <td>36</td> </tr> <tr> <td>$22 < t \leq 26$</td> <td>7</td> <td>43</td> </tr> <tr> <td>$26 < t \leq 30$</td> <td>2</td> <td>45</td> </tr> </tbody> </table>	Time taken (<i>t</i>) (in minutes)	Number of children	Cumulative frequency	$2 < t \leq 6$	2	2	$6 < t \leq 10$	10	12	$10 < t \leq 14$	9	21	$14 < t \leq 18$	7	28	$18 < t \leq 22$	8	36	$22 < t \leq 26$	7	43	$26 < t \leq 30$	2	45	✓ first 4 cum freq correct ✓ last 3 cum freq correct (2)
Time taken (<i>t</i>) (in minutes)	Number of children	Cumulative frequency																								
$2 < t \leq 6$	2	2																								
$6 < t \leq 10$	10	12																								
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$18 < t \leq 22$	8	36																								
$22 < t \leq 26$	7	43																								
$26 < t \leq 30$	2	45																								
1.4	<p style="text-align: center;">CUMULATIVE FREQUENCY GRAPH (OGIVE)</p>	✓ plotting cum freq at upper limits correctly (all points) ✓ shape (smooth) ✓ grounding (2;0) (3)																								
1.5	On graph at the y-value of 22,5 or 23 Median = ± 15 minutes. <div style="border: 1px solid black; padding: 2px; display: inline-block; margin-left: 20px;">Answer only: full marks</div>	☞ graph ☞ answer (2)																								
		[10]																								





QUESTION/VRAAG 2



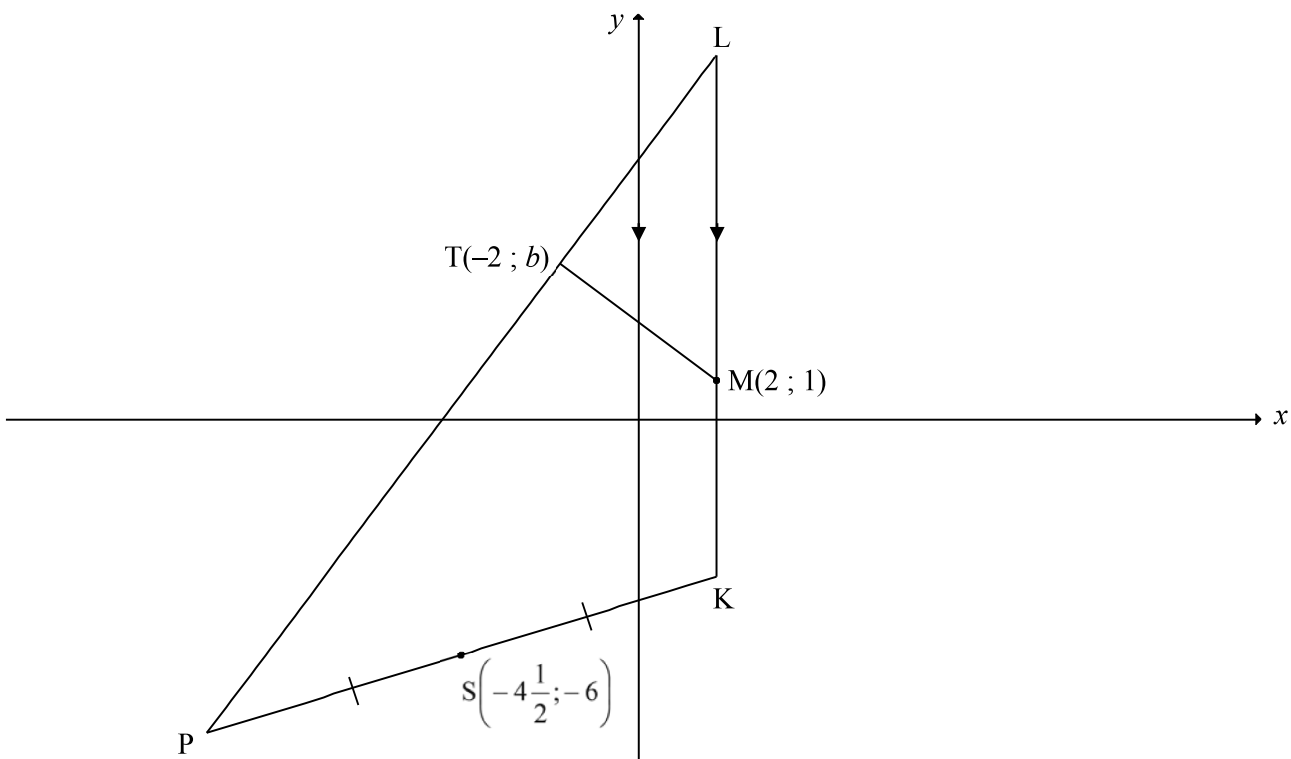
2.1.1	Midpoint of EC: $= \left(\frac{-2+2}{2} ; \frac{0+(-3)}{2} \right) = \left(0 ; \frac{-3}{2} \right)$	☞ x value ☞ y value (2)
2.1.2	$m_{DC} = \frac{-3 - (-5)}{2 - (-2)} \text{ OR } \frac{-5 - (-3)}{-2 - 2}$ $= \frac{2}{4} = \frac{1}{2}$ <div style="border: 1px solid black; padding: 2px; display: inline-block; margin-left: 100px;">Answer only: full marks</div>	☞ substitution ☞ answer (2)
2.1.3	$m_{AB} = \frac{1}{2} \quad [AB \parallel DC]$ $y = \frac{1}{2}x + c$ $0 = \frac{1}{2}(-2) + c \quad \text{OR} \quad y - y_1 = \frac{1}{2}(x - x_1)$ $c = 1 \quad \quad \quad y - 0 = \frac{1}{2}(x - (-2))$ $\therefore y = \frac{1}{2}x + 1$	☞ $m_{AB} = \frac{1}{2}$ ☞ substitution of (-2; 0) ☞ equation (3)
2.1.4	$\tan \alpha = m_{AB} = \frac{1}{2}$ $\alpha = 26,57^\circ$ $\theta = 90^\circ + 26,57^\circ \quad [\text{ext } \angle \text{ of } \Delta]$ $= 116,57^\circ$	☞ $\tan \alpha = \frac{1}{2}$ ☞ value of α ☞ value of θ (3)



2.2	$B(0 ; 1)$ $m_{BC} = \frac{1 - (-3)}{0 - 2} \quad \text{OR} \quad m_{BC} = \frac{(-3) - 1}{2 - 0}$ $= -2 \qquad \qquad \qquad = -2$ $m_{AB} \times m_{BC} = \frac{1}{2} \times -2$ $= -1$ $\therefore AB \perp BC$	<p>☞ coordinates of B</p> <p>☞ $m_{BC} = -2$</p> <p>☞ product of gradients = -1</p> <p style="text-align: right;">(3)</p>
2.3.1	$\hat{A}BC = 90^\circ$ $\therefore EC \text{ is diameter [converse: } \angle \text{ in semi circle]}$ $\therefore \text{centre of circle} = \begin{pmatrix} 0 ; -\frac{3}{2} \end{pmatrix}$	<p>☞ answer</p> <p style="text-align: right;">(1)</p>
2.3.2	$(x-0)^2 + \left(y + \frac{3}{2}\right)^2 = r^2$ $(-2-0)^2 + \left(0 + \frac{3}{2}\right)^2 = r^2 \quad \text{OR} \quad (2-0)^2 + \left(-3 - \left(\frac{-3}{2}\right)\right)^2 = r^2$ $\text{OR } (0-0)^2 + \left(1 - \left(\frac{-3}{2}\right)\right)^2 = r^2$ $\text{OR } r = \frac{EC}{2} = \frac{\sqrt{(-2-2)^2 + (0-(-3))^2}}{2}$ $\text{OR } r = 1 - \left(-\frac{3}{2}\right)$ $\therefore r^2 = \frac{25}{4} \quad \text{or } r = \frac{5}{2}$ $x^2 + \left(y + \frac{3}{2}\right)^2 = \frac{25}{4}$	<p>☞ substitution of centre</p> <p>☞ correct substitution of E(-1 ; 0), B(0 ; 1) or C(2 ; -3) to calculate r^2 or r</p> <p>☞ value of r^2 or r</p> <p>☞ equation</p> <p style="text-align: right;">(4)</p>
[18]		

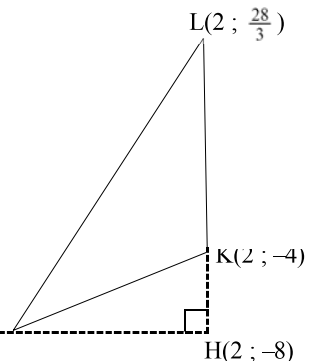


QUESTION/VRAAG 3



3.1	$(x-2)^2 + (y-1)^2 = 25$ $(-2-2)^2 + (b-1)^2 = 25$ $(b-1)^2 = 9$ OF $16 + b^2 - 2b + 1 = 25$ $b-1 = \pm 3$ $\therefore b=4$ or $b=-2$	$(x-2)^2 + (y-1)^2 = 25$ $(-2-2)^2 + (b-1)^2 = 25$ $b^2 - 2b - 8 = 0$ $\therefore b=4$ or $b=-2$	☞ equation of the circle ☞ substitution of point T ☞ simplification ☞ answer (4)
3.2.1	$K(2; 1-5)$ $\therefore K(2; -4)$	Answer only: full marks	☞ x value ☞ y value (2)
3.2.2	$m_{MT} = \frac{4-1}{-2-2} = -\frac{3}{4}$ $m_{PL} = \frac{4}{3}$ [radius \perp tangent] $y = \frac{4}{3}x + c$ $4 = \frac{4}{3}(-2) + c$ $c = \frac{20}{3}$ $y = \frac{4}{3}x + \frac{20}{3}$	$m_{MT} = -\frac{3}{4}$ $m_{PL} = \frac{4}{3}$ ☞ substitution of m_{PL} and the point T ☞ equation (4)	



	<p>OR</p> $m_{MT} = \frac{4-1}{-2-2} = -\frac{3}{4}$ $m_{PL} = \frac{4}{3} \quad [\text{radius} \perp \text{tangent}]$ $y - y_1 = \frac{4}{3}(x - x_1)$ $y - 4 = \frac{4}{3}(x + 2)$ $y = \frac{4}{3}x + \frac{20}{3}$ <p>OR</p> <p>P(-11 ; -8)</p> $m_{PL} = \frac{4 - (-8)}{-2 - (-11)}$ $= \frac{4}{3}$ $y = \frac{4}{3}x + c$ $-8 = \frac{4}{3}(-11) + c$ $c = \frac{20}{3}$ $y = \frac{4}{3}x + \frac{20}{3}$	<p>☞ m_{MT}</p> <p>☞ $m_{PL} = \frac{4}{3}$</p> <p>☞ substitution of m_{PL} and the point T</p> <p>☞ equation (4)</p> <p>☞ coordinates of P</p> <p>☞ $m_{PL} = \frac{4}{3}$</p> <p>☞ substitution of m_{PL} and the point P or T</p> <p>☞ equation (4)</p>
<p>3.2.3</p>	$y = \frac{4}{3}(2) + \frac{20}{3} = \frac{28}{3}$ <p>$(2; \frac{28}{3})$ and K(2 ; -4): $LK = \frac{28}{3} - (-4) = \frac{40}{3}$</p> <p><u>Coordinates of P:</u></p> $\frac{x+2}{-4} = -4 \frac{1}{3} \quad \text{and} \quad \frac{y-4}{-6} = -6$ <p>$\therefore x = -11 \quad y = -8$</p> <p>$\therefore P(-11; -8)$</p> <p>$\perp$ height (PH) = $2 - (-11) = 13$</p> <p>Area $\Delta PKL = \frac{1}{2}(LK)(PH)$</p> $= \frac{1}{2} \left \frac{40}{3} \right 13$ $= \frac{260}{3} \quad \text{OR} \quad 86,67 \text{ square units}$ 	<p>☞ $y = \frac{28}{3}$</p> <p>☞ length of LK</p> <p>☞ x_P ☞ y_P</p> <p>☞ length of \perp height</p> <p>☞ substitution into the area formula</p> <p>☞ answer (7)</p>

<p>3.2.3</p>	<p>OR</p> $y = -\frac{4}{3}(2) + \frac{20}{3} = \frac{28}{3}$ $\left(2; \frac{28}{3}\right) \text{ and } K(2; -4): \text{LK} = \frac{28}{3} - (-4) = \frac{40}{3}$ <p><u>Coordinates of P:</u></p> $\frac{x+2}{1} = -\frac{1}{1} \quad \frac{y-4}{1} = -$ $\therefore x = -11 \quad y = -8$ $\therefore P(-11; -8)$ $PK^2 = (-11-2)^2 + (-8-(-4))^2$ $PK = \sqrt{(-11-2)^2 + (-8-(-4))^2} = \sqrt{185}$ $\tan \theta = \frac{4}{13} \therefore \theta = 17,1027\dots^\circ$ $\therefore \widehat{PKL} = 90^\circ + 17,1027\dots^\circ = 107,1^\circ$ $\text{Area } \Delta PKL = \frac{1}{2}(PK)(LK) \sin \widehat{PKL}$ $= \frac{1}{2}(\sqrt{185})\left(\frac{40}{3}\right) \sin 107,1^\circ$ $= 86,67 \text{ square units}$	<p>$y = \frac{28}{3}$</p> <p>length of LK</p> <p>x_P y_P</p> <p>\widehat{PKL}</p> <p>substitution into the area rule</p> <p>answer</p> <p>(7)</p>
<p>3.3</p>	<p>The centres of the two circles lie on the same vertical line</p> $x = 2 \text{ and the sum of the radii} = 10$ $n-1 = 10 \quad \text{or} \quad 1-n = 10$ $n=11 \quad \text{or} \quad n = -9$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Answer only: full marks</p> </div>	<p>correct method</p> <p>sum of radii = 10</p> <p>$n=11$ $n = -9$</p> <p>(4)</p>
<p>[21]</p>		

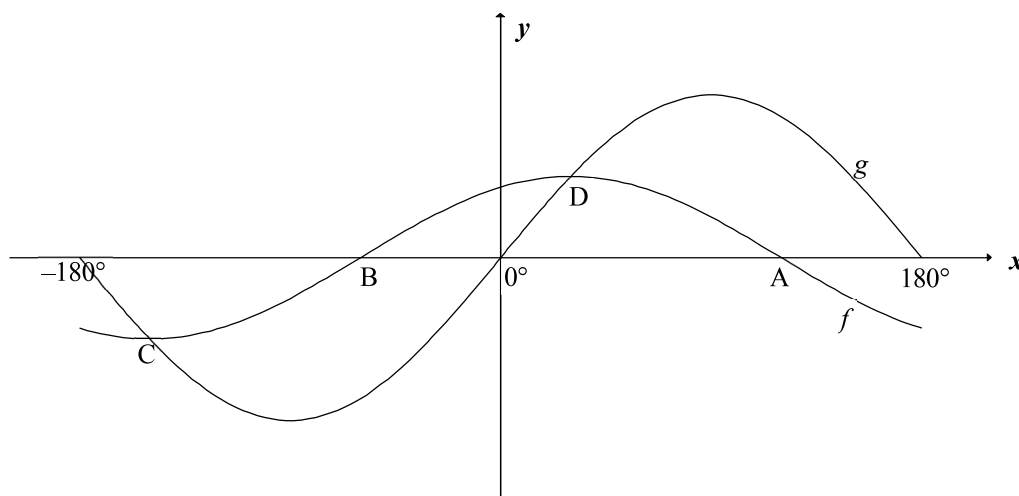


QUESTION/VRAAG 4

4.1.1	$\sin 191^\circ$ $= -\sin 11^\circ$	$\spadesuit -\sin 11^\circ$ (1)
4.1.2	$\cos 22^\circ$ $= \cos(2 \times 11^\circ)$ $= 1 - 2\sin^2 11^\circ$	\spadesuit answer (1)
4.2	$\cos(x-180^\circ) + \sqrt{2} \sin(x+45^\circ)$ $= -\cos x + \sqrt{2}(\sin x \cos 45^\circ + \cos x \sin 45^\circ)$ $= -\cos x + \sqrt{2} \left(\sin x \left(\frac{1}{\sqrt{2}} \right) + \cos x \left(\frac{1}{\sqrt{2}} \right) \right)$ $= -\cos x + \sin x + \cos x$ $= \sin x$ OR $\cos(x-180^\circ) + \sqrt{2} \sin(x+45^\circ)$ $= -\cos x + \sqrt{2}(\sin x \cos 45^\circ + \cos x \sin 45^\circ)$ $= -\cos x + \sqrt{2} \left(\sin x \left(\frac{\sqrt{2}}{2} \right) + \cos x \left(\frac{\sqrt{2}}{2} \right) \right)$ $= -\cos x + \sin x + \cos x$ $= \sin x$	$\spadesuit -\cos x$ \spadesuit expansion \spadesuit special angle ratios \spadesuit simplification of last 2 terms \spadesuit answer (5)
4.3	$\sin P + \sin Q = \sin P + \cos P$ $(\sin P + \cos P)^2 = \left(\frac{7}{5} \right)^2$ $\sin^2 P + 2 \sin P \cos P + \cos^2 P = \frac{49}{25}$ $2 \sin P \cos P = \frac{49}{25} - 1$ $\sin 2P = \left(\frac{49 - 25}{25} \right)$ $= \frac{24}{25}$	$\spadesuit \sin Q = \cos P$ \spadesuit squaring \spadesuit expansion $\spadesuit \sin^2 P + \cos^2 P = 1$ \spadesuit answer (5)
		[12]



5.1	$\cos(x - 30^\circ) = 2 \sin x$ $\cos x \cos 30^\circ + \sin x \sin 30^\circ = 2 \sin x$ $\frac{\sqrt{3}}{2} \cos x + \frac{1}{2} \sin x = 2 \sin x$ $\frac{\sqrt{3}}{2} \cos x = \frac{3}{2} \sin x$ $\tan x = \frac{\sqrt{3}}{3}$ $x = 30^\circ + k \cdot 180^\circ; \quad k \in \mathbb{Z}$ <p>OR</p> $x = 30^\circ + k \cdot 360^\circ \text{ or } x = 210^\circ + k \cdot 360^\circ; \quad k \in \mathbb{Z}$	<ul style="list-style-type: none"> ☞ expansion ☞ special \angle s ☞ simplification ☞ equation in tan ☞ 30° ☞ $k \cdot 180^\circ; k \in \mathbb{Z}$ OR ☞ 30° and 210° ☞ $k \cdot 360^\circ; k \in \mathbb{Z}$ <p style="text-align: right;">(6)</p>
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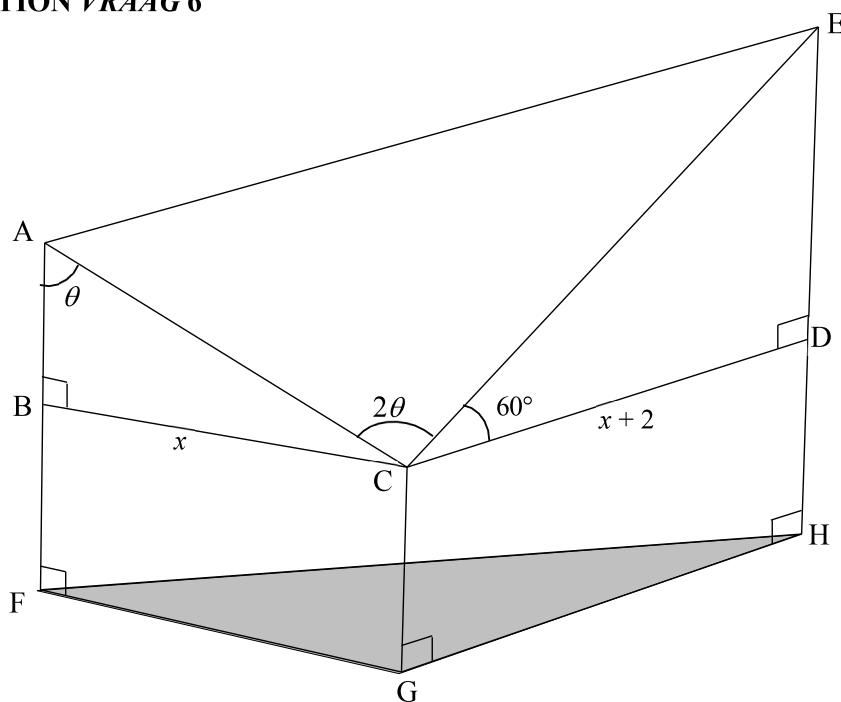


5.2.1(a)	A(120° ; 0)	☞ answer (1)
5.2.1(b)	C(-150° ; -1)	☞ x value ☞ y value (2)
5.2.2(a)	$x \in (-90^\circ ; 30^\circ)$ OR $-90^\circ < x < 30^\circ$	☞ endpoints ☞ correct interval (2)
5.2.2(b)	$x \in (-160^\circ ; 20^\circ)$ OR $-160^\circ < x < 20^\circ$	☞ endpoints ☞ correct interval (2)
5.2.3	$y = 2^{2 \sin x + 3}$ Range of $y = 2 \sin x$: $y \in [-2 ; 2]$ OR $-2 \leq y \leq 2$ Range of $y = 2 \sin x + 3$: $y \in [1 ; 5]$ OR $1 \leq y \leq 5$ Range: $y = 2^{2 \sin x + 3}$: $y \in [2 ; 32]$ OR $2 \leq y \leq 32$	☞ 1 ☞ 5 ☞ 2 ☞ 32 ☞ correct interval (5)

Answer only: full marks



/ QUESTION VRAAG 6



6.1.1	$\sin \theta = \frac{x}{AC}$ $AC = \frac{x}{\sin \theta}$ <p style="text-align: center;">OR</p> $\frac{\sin \theta}{x} = \frac{\sin 90^\circ}{AC}$ $AC = \frac{x}{\sin \theta}$	<ul style="list-style-type: none"> ☞ trig ratio ☞ simplification <p style="text-align: right;">(2)</p>
6.1.2	$\cos 60^\circ = \frac{x+2}{CE}$ $CE = \frac{x+2}{\cos 60^\circ}$ $= \frac{x+2}{\frac{1}{2}} = 2(x+2)$ <p style="text-align: center;">OR</p> $\frac{\sin 30^\circ}{x+2} = \frac{\sin 90^\circ}{CE}$ $CE = \frac{x+2}{\sin 30^\circ}$ $= 2(x+2)$	<ul style="list-style-type: none"> ☞ trig ratio ☞ making CE the subject <p style="text-align: right;">(2)</p>
6.2	$\text{Area } \triangle ACE = \frac{1}{2} AC \cdot EC \cdot \sin \hat{A} C E$ $= \frac{1}{2} \left(\frac{x}{\sin \theta} \right) (2(x+2)) \sin 2\theta$ $= \frac{x(x+2) \times 2 \sin \theta \cos \theta}{\sin \theta}$ $= 2x(x+2) \cos \theta$	<ul style="list-style-type: none"> ☞ use area rule correctly ☞ substitution of $\frac{x}{\sin \theta} (2(x+2))$ ☞ substitution of $\sin 2\theta$ <p style="text-align: right;">(3)</p>

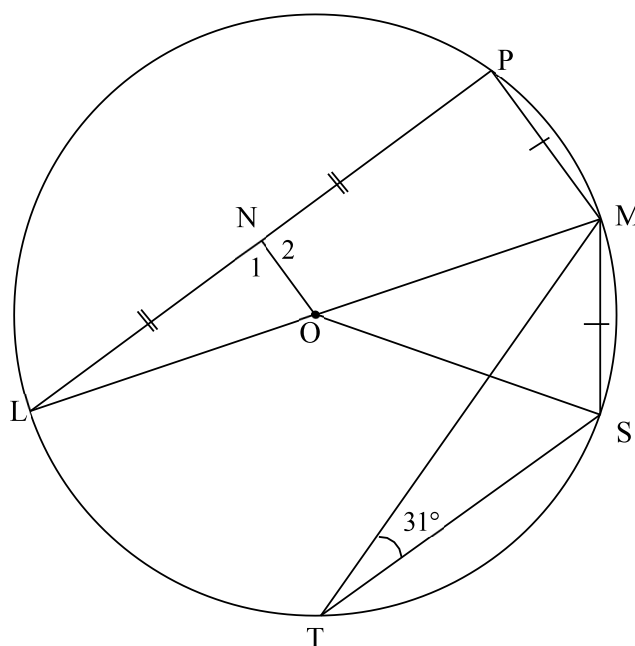


6.3	$EC = 2(12 + 2) = 28$ $AE^2 = AC^2 + EC^2 - 2(AC)(EC)\cos\hat{A}CE$ $= \left(\frac{12}{\sin 55^\circ} \right)^2 + 28^2 - 2 \left(\frac{12}{\sin 55^\circ} \right) (28) \cos 110^\circ$ $AE = 35,77m$	<ul style="list-style-type: none"> ☞ EC ☞ use cosine rule correctly ☞ substitution ☞ answer <p style="text-align: right;">(4)</p>
		[11]



QUESTION/VRAAG 7

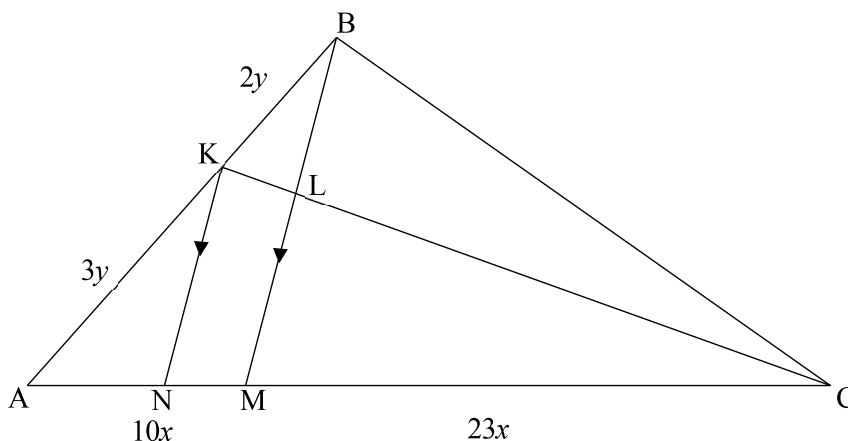
7.1



7.1.1(a)	$\widehat{MÔS} = 62^\circ$ [\angle at centre = $2 \times \angle$ at circumf/middelpts $\angle = 2$ omtreks \angle]	✓ S ✓ R (2)
7.1.1(b)	$\widehat{L} = 31^\circ$ [equal chords; equal \angle s / = koorde; = \angle e]	✓ S ✓ R (2)
7.1.2	<p>LN = NP and LO = OM</p> <p>$\therefore ON = \frac{1}{2} PM$ [midpoint theorem/middelpuntstelling]</p> <p>$\therefore ON = \frac{1}{2} MS$ [PM = MS]</p> <p>OR</p> <p>$\widehat{N}_1 = 90^\circ$ [line from centre to midpt chord/lyn v midpt na midpt kd]</p> <p>$\widehat{P} = 90^\circ$ [\angle in semi-circle/\angle in halfsirkel]</p> <p>\widehat{L} is common/gemeen</p> <p>$\therefore \triangle NLO \parallel \triangle PLM$ ($\angle \angle \angle$)</p> <p>$\frac{NL}{PL} = \frac{NO}{PM} = \frac{1}{2}$</p> <p>$\therefore ON = \frac{1}{2} PM$</p> <p>$\therefore ON = \frac{1}{2} MS$ [PM = MS]</p>	<p>✓ LO = OM</p> <p>✓ S ✓ R</p> <p>✓ S</p> <p>(4)</p> <p>✓ S R</p> <p>✓ S/R</p> <p>✓ S</p> <p>✓ S</p> <p>(4)</p>



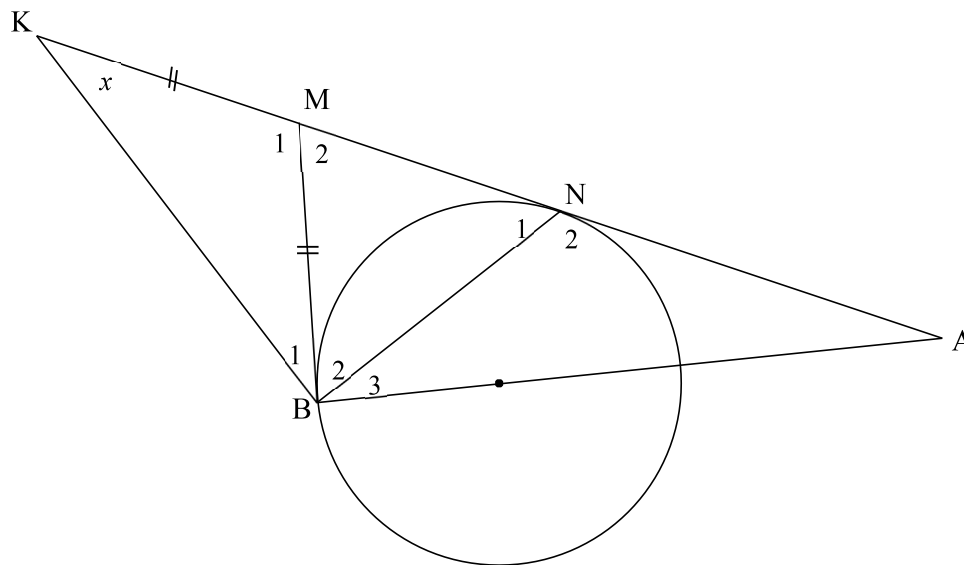
7.2



7.2.1	$\frac{AN}{AM} = \frac{AK}{AB}$ [line one side of Δ OR prop theorem; $KN \parallel BM$ / lyn sy van Δ OR eweredigheidst; $KN \parallel BM$]	✓ R ✓ S (2)
7.2.2	$\frac{AM}{MC} = \frac{10x}{23x}$ [given] $AM = 5y = 10x \quad \therefore y = 2x$ $\frac{LC}{KL} = \frac{MC}{NM}$ [line one side of Δ OR prop theorem; $KN \parallel LM$ / lyn sy van Δ OR eweredigheidst; $KN \parallel BM$]	✓ S ✓ R ✓ S (3)
	OR $\frac{AM}{MC} = \frac{10x}{23x}$ [given] $\frac{AN}{MN} = \frac{3y}{2y} = \frac{6x}{4x}$ $\frac{LC}{KL} = \frac{MC}{NM}$ [line one side of Δ OR prop theorem; $KN \parallel LM$ / lyn sy van Δ OR eweredigheidst; $KN \parallel BM$]	✓ S ✓ R ✓ S (3)
		[13]



QUESTION/VRAAG 8



<p>8.1</p>	<p>$\hat{B}_1 = x$ [\angle's opp = sides/ \anglee teenoor = sye] $\hat{M}_2 = 2x$ [ext \angle of Δ] OR $\hat{M}_1 = 180^\circ - 2x$ [\angles of Δ] $BM = MN$ [2 tans from a common point/raaklyne vanuit dieselfde punt] $\hat{N}_1 = \frac{180^\circ - 2x}{2} = 90^\circ - x$ [\angle's opp = sides/ \anglee teenoor = sye] OR $NM = BM$ [2 tans from a common point/raaklyne vanuit dieselfde punt] $\hat{B}_2 = \hat{N}_1$ [\angle's opp = sides/ \anglee teenoor = sye] $\hat{B}_1 = x$ [\angle's opp = sides/ \anglee teenoor = sye] In ΔKBN: $x + x + \hat{B}_2 + \hat{N}_1 = 180^\circ$ [sum of \angle's of Δ] $2x + 2\hat{N}_1 = 180^\circ$ $x + \hat{N}_1 = 90^\circ$ $\hat{N}_1 = 90^\circ - x$</p>	<p>✓S ✓S ✓R ✓S ✓R ✓ answer (6) ✓S ✓R ✓S ✓R ✓S ✓ answer (6)</p>
<p>8.2</p>	<p>$M\hat{B}A = \hat{B}_2 + \hat{B}_3 = 90^\circ$ [tangent \perp diameter/raaklyn \perp middellyn] $\hat{B}_3 = 90^\circ - \hat{B}_2$ $= 90^\circ - (90^\circ - x) = x$ $\hat{B}_3 = \hat{K} = x$ $\therefore AB$ is a tangent/raaklyn converse tan-chord theorem/ omgekeerde raakl koordst]]</p>	<p>✓S ✓R ✓S ✓S ✓R (5)</p>

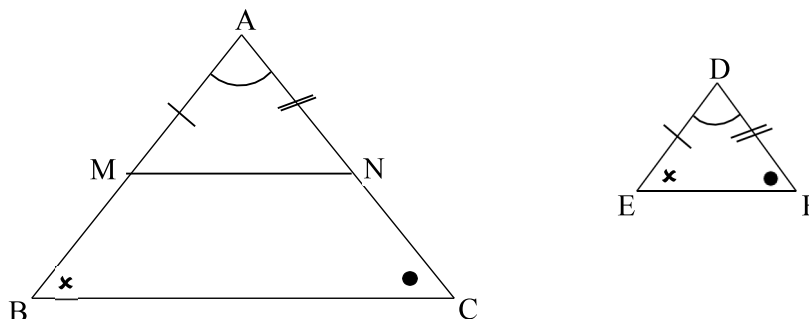


	<p>OR</p> <p>$\hat{B}_2 = \hat{N}_1$</p> <p>$\hat{B}_1 + \hat{B}_2 = x + (90^\circ - x) = 90^\circ$</p> <p>$\therefore$ KN is diameter/<i>middel lyn</i> [converse \angle in semi-circle/ <i>omgekeerde \angle in halfsirkel</i>]</p> <p>$M\hat{B}A = \hat{B}_2 + \hat{B}_3 = 90^\circ$ [tangent \perp diameter]</p> <p>\therefore AB is a tangent/<i>raaklyn</i> converse tan-chord theorem/ <i>omgekeerde raakl koordst</i>]</p>	<p>✓ S</p> <p>✓ R</p> <p>✓ S ✓ R</p> <p>✓ R</p> <p>(5)</p>
		[11]



QUESTION/VRAAG 9

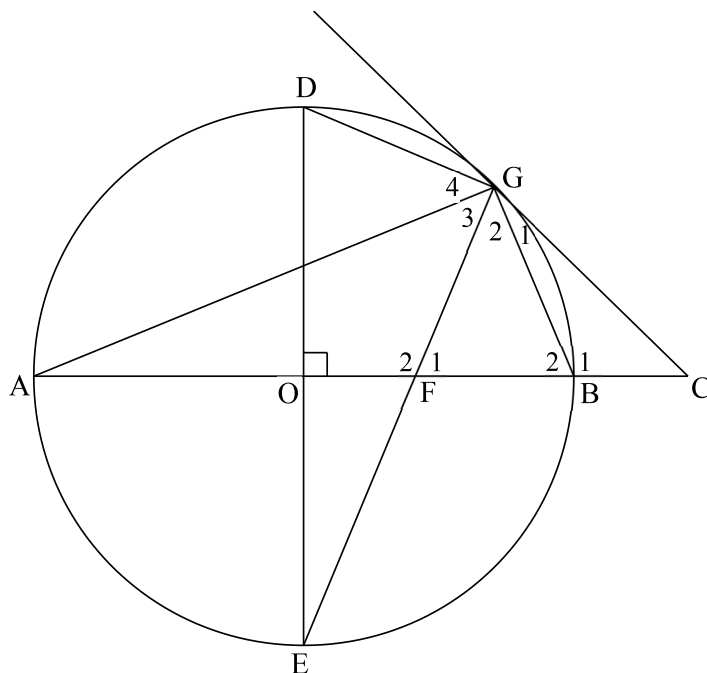
9.1



9.1	<p>Constr: Let M and N lie on AB and AC respectively such that $AM = DE$ and $AN = DF$. Draw MN.</p> <p>Konstr: Merk M en N op AB en AC onderskeidelik af sodanig dat $AM = DE$ en $AN = DF$. Verbind MN.</p> <p>Proof:</p> <p>In $\triangle AMN$ and $\triangle DEF$ $AM = DE$ [Constr] $AN = DF$ [Constr] $\hat{A} = \hat{D}$ [Given] $\therefore \triangle AMN \cong \triangle DEF$ (SAS) $\therefore \hat{M} = \hat{E}$ $MN \parallel BC$ [corresp \angle's are equal/ooreenkomstige \anglee =] $\frac{AM}{AB} = \frac{AN}{AC}$ [line \parallel one side of \triangle OR prop theorem; $MN \parallel BC$] $\therefore \frac{AM}{DE} = \frac{AN}{DF}$ [AM = DE and AN = DF]</p>	<p>✓ Constr / Konstr</p> <p>✓ $\triangle AMN \cong \triangle DEF$</p> <p>✓ SAS</p> <p>✓ $MN \parallel BC$ and R</p> <p>✓ $\frac{AM}{DE} = \frac{AN}{DF}$ ✓ R</p> <p>(6)</p>
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9.2



<p>9.2.1(a)</p>	<p>$D\hat{O}B=90^\circ$ $D\hat{G}F=\hat{G}_3+\hat{G}_4=90^\circ$ [∠ in semi-circle/∠ in halfsirkel] $D\hat{O}B+D\hat{G}F=180^\circ$ $\therefore DGFO$ is a cyclic quad. [converse: opp ∠s of cyclic quad/ <i>omgekeerde teenoorst ∠e v koordevh</i>] OR \angles of quad = 180°/∠e van koordevh = 180° OR $E\hat{O}B=90^\circ$ $D\hat{G}F=\hat{G}_3+\hat{G}_4=90^\circ$ [∠ in semi-circle/∠ in halfsirkel] $E\hat{O}B=D\hat{G}F$ $\therefore DGFO$ is a cyclic quad. [converse: ext ∠ = opp int ∠/ <i>omgekeerde buite∠ = teenoorst ∠</i>] OR ext∠ of quad = opp int ∠/ buite∠ v vh = teenoorst ∠</p>	<p>✓ S ✓ R ✓ R (3) ✓ S ✓ R ✓ R (3)</p>
<p>9.2.1(b)</p>	<p>$\hat{F}_1=\hat{D}$ [ext ∠ of cyclic quad/buite∠ v koordevh] $\hat{G}_1+\hat{G}_2=\hat{D}$ [tan-chord theorem/raakl koordst] $\therefore \hat{F}_1=\hat{G}_1+\hat{G}_2$ $\therefore GC=CF$ [sides opp equal ∠s/sye teenoor = ∠e]</p>	<p>✓ S ✓ R ✓ S ✓ R ✓ R (5)</p>



9.2.2(a)	$AB = DE = 14$ [diameters/middellynne] $\therefore OB = 7$ units $\therefore BC = OC - OB = 11 - 7$ $= 4$ units <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 100px;">Answer only: full marks</div>	✓ S ✓ S ✓ S (3)
9.2.2(b)	In $\triangle CGB$ and $\triangle CAG$ $\hat{G}_1 = \hat{A} = x$ [tan-chord theorem/raakl koordst] $\hat{C} = \hat{C}$ [common] $\triangle CGB \parallel \triangle CAG$ [\angle, \angle, \angle] $\frac{CG}{CA} = \frac{CB}{CG}$ $\frac{CG}{18} = \frac{4}{CG}$ $CG^2 = 72$ $CG = \sqrt{72}$ or $6\sqrt{2}$ or 8,49 units	✓ S/R ✓ S ✓ S ✓ CA = 18 ✓ answer (5)
9.2.2(c)	$OF = OC - FC$ $= 11 - \sqrt{72}$ $\tan E = \frac{OF}{OE}$ $= \frac{11 - \sqrt{72}}{7} = 0,36$ $\hat{E} = 19,76^\circ$ OR $OF = OC - FC$ $= 11 - \sqrt{72}$ $FE^2 = OE^2 + OF^2$ $= 7^2 + (11 - \sqrt{72})^2$ $FE = 7,437.. = 7,44$ $\cos E = \frac{OE}{FE}$ $= \frac{7}{7,44} = 0,94$ $\hat{E} = 19,76^\circ$ <div style="display: inline-block; vertical-align: middle; margin-left: 20px;"> OR $\sin E = \frac{OF}{FE}$ $= \frac{11 - \sqrt{72}}{7,44} = 0,338$ $\hat{E} = 19,76^\circ$ </div>	✓ OF ✓ trig ratio ✓ substitution ✓ answer (4) ✓ OF ✓ trig ratio ✓ substitution ✓ answer (4)
		[26]
		TOTAL/TOTAAL: 140

