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# CAPRICORN SOUTH DISTRICT

### **GRADE 12**

# MATHEMATICS PRE FORMAL TEST TEST 1

**MARKS: 100** 

TIME: 2 Hours

**DATE:** 06/03/2024

This question paper consists of 6 pages

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#### INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of 6 Questions.
- 2. Answer ALL the questions.
- 3. Clearly show ALL calculations, diagrams and graphs that you have used in determining your answers.
- 4. Answers only will NOT necessarily be awarded full marks.
- 5. An approved scientific calculator (non-programmable and non-graphical) may be used, unless stated otherwise.
- 6. If necessary, answers should be rounded off to TWO decimal places, unless stated otherwise.
- 7. Diagrams are NOT necessarily drawn to scale.
- 8. Number your answers correctly according to the numbering system used in this question paper.
- 9. It is in your own interest to write legibly and to present your work neatly.



#### **QUESTION 1**

1.1 Solve for *x*:

$$1.1.1 \quad 2 + 3x = x - 26 \tag{2}$$

$$1.1.2 \quad 2x^2 + x - 15 = 0 \tag{3}$$

1.1.3 
$$3x^2 + 2x - 4 = 0$$
 (round off your answer to TWO decimal places) (4)

$$1.1.4 \quad (x-1)^2 > 4 \tag{4}$$

$$1.1.5 \quad \sqrt{-7x + 2} = -x + 2 \tag{4}$$

1.2 Solve for x and y if they satisfy the following equations simultaneously:

$$x - y = -1$$

$$x^2 - 2xy + 3y^2 = 9 (6)$$

[23]

#### **QUESTION 2**

- 2.1 Consider the quadratic sequence 3; 9; 17; 27; ...
- Determine an expression for the n<sup>th</sup> term of the sequence. 2.1.1 (3)
- 2.1.2 What is the value of the first term of the sequence that is greater than 269? (3)
- 2.2 Given the following arithmetic sequence: p + 3; 2p - 3; p - 5; ...
- 2.2.1 Determine the value of p. (2)
- Determine the 10<sup>th</sup> term of the sequence. (2)
- How many terms of the sequence must be added to give a sum of -984? (3)

[13]

(4)

#### **Question 3**

A certain quadratic pattern has the following features:

- $T_1 = x$
- $T_2 = 18$  $T_4 = 4x$
- $T_3 T_2 = 10$

Determine the value of x.



- 2.2 Given the geometric series:  $15 + p + \frac{5}{3} + \frac{5}{9} + \dots$ 
  - 2.2.1 Determine the value of p. (3)
  - 2.2.2 Calculate the sum of the first 8 terms of the series. (3)
  - 2.2.3 Explain why the series is convergent. (2)

2.2.4 Evaluate 
$$\sum_{n=1}^{\infty} 5(3^{2-n})$$
 (3)

[15]

#### **Question 3**

Consider the function:  $g(x) = \frac{-4}{x+1} - 3$ 

- 3.1 Write down the range of g. (1)
- 3.2 Write down the y-intercept of g. (1)
- 3.3 Calculate the *x*-intercept of g. (2)
- 3.4 Sketch the graph of g, clearly indicating the intercepts with the axes and the asymptotes. (3)

[07]

#### **QUESTION 4**

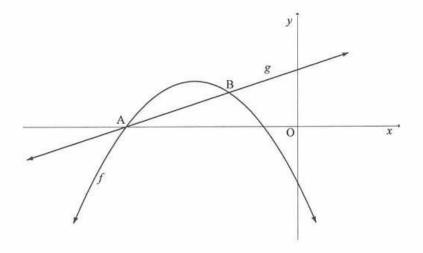
- 4.1 Given the function  $p(x) = \left(\frac{1}{3}\right)^x$ .
  - 4.1.1 Is p an increasing or decreasing function? (1)
  - 4.1.2 Determine  $p^{-1}$ , the inverse of p, in the form y = ... (2)
  - 4.1.3 Write down the domain of  $p^{-1}$ . (1)
  - 4.1.4 Write down the equation of the asymptote of p(x) 5. (1)
- 4.2 Given:  $f(x) = \frac{4}{x-1} + 2$ 
  - 4.2.1 Write down the equations of the asymptotes of f. (2)
  - 4.2.2 Calculate the x-intercept of f. (2)
  - 4.2.3 Sketch the graph of f, label all asymptotes and indicate the intercepts with the axes. (4)
  - 4.2.4 Use your graph to determine the values of x for which  $\frac{4}{x-1} \ge -2$ . (2)
  - 4.2.5 Determine the equation of the axis of symmetry of f(x-2), that has a negative gradient. (3)

    [18]



#### **QUESTION 5**

The graphs of the functions  $f(x) = -(x+3)^2 + 4$  and g(x) = x+5 are drawn below. The graphs intersect at A and B.

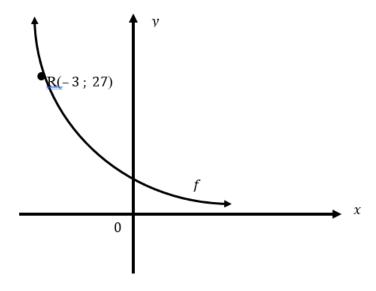


- 5.1 Write down the coordinates of the turning point of f. (2)
- 5.2 Write down the range of f. (1)
- Show that the x-coordinates of A and B are -5 and -2 respectively. (4)
- Hence, determine the values of c for which the equation  $-(x+c+3)^2+4=(x+c)+5$  has ONE negative and ONE positive root. (2)
- 5.5 The maximum distance between f and g in the interval  $x_A < x < x_B$  is k. If h(x) = g(x) + k, determine the equation of h in the form h(x) = ... [5]



### **Question 6**

The graph of  $f(x) = a^x$  is drawn below. The point R(-3; 27) lies on f.



6.1 Write down the domain and range of f (2)

6.2 Write down the coordinates of the y – intercept of f. (2)

6.3 Calculate the value of a. (2)

6.4 Determine the equation of  $f^{-1}$ , the inverse of f, in the form  $y = \dots$  (2)

6.5 Write down the values of x for which  $f^{-1}(x) \ge -3$ . (2)

[10]

//100//

