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AMENDMENT TO MARKING GUIDELINES

PREPARATORY EXAMINATION /
VOORBEREIDENDE EKSAMEN 2023

FOR ATTENTION / VIR AANDAG: THE CHIEF INVIGILATOR / DIE HOOF TOESIGHOUER

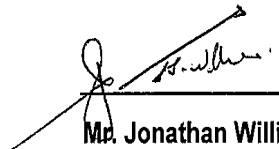
SUBJECT / VAK	MATHEMATICS / WISKUNDE
SUBJECT CODE / VAKKODE	10611
PAPER / VRAESTEL	1
DATE OF EXAMINATION / DATUM VAN EKSAMEN	8 SEPTEMBER 2023

The **MATHEMATICS / WISKUNDE** (Paper / *Vraestel* 1) written on **8 September 2023** has reference. It has come to our attention that there was an anomaly in the question paper which rendered **Question / Vraag 9.2** ambiguous.

To ensure that your candidates are not disadvantaged and prejudiced in way, you are advised to please ask Educators to ignore **Question / Vraag 9.2** when **marking**.

In other words, the paper must be marked out of a total of 145 instead of 150 and then the learners' marks must be converted back to a mark out of 150. E.g. Should a learner have attained 65/145, then that mark is recalculated as 67/150.

<p>Use the formula: $\frac{a}{145} \times 100 = b$. Then, $\frac{b}{100} \times 150 = c$</p> <p><i>c</i> is the mark that is entered into SASAMS out of 150.</p>
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 Mr. Jonathan Williams

DIRECTOR: EXAMINATIONS MANAGEMENT

9 September 2023





PREPARATORY EXAMINATION

2023

MARKING GUIDELINES

MATHEMATICS (PAPER 1) (10611)

21 pages

INSTRUCTIONS AND INFORMATION:

A – Accuracy

CA – Continued Accuracy

S – Statement

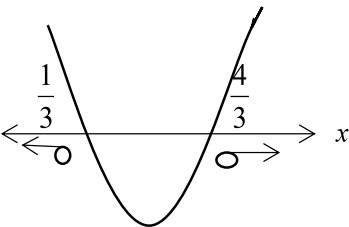
R – Reason

S and R – Statement and Reason

NOTE:

- If a candidate answered a question TWICE, mark only the FIRST attempt.
- If a candidate crossed OUT an answer and did not redo it, mark the crossed-out answer.
- Consistent accuracy applies to ALL aspects of the marking guidelines.
- It is UNACCEPTABLE to assume values/answers in order to solve a question.

QUESTION 1

1.1	1.1.1	$(2x+1)^2 - 4 = 0$ $4x^2 + 4x + 1 - 4 = 0$ $4x^2 + 4x - 3 = 0$ $(2x+3)(2x-1) = 0$ $x = -\frac{3}{2}$ or $x = \frac{1}{2}$	✓ standard form ✓ factors ✓ answers		
		OR			
		$(2x+1)^2 - 4 = 0$ $2x+1 = \pm\sqrt{4}$ $2x+1 = \pm 2$ $2x = \pm 2 - 1$ $2x = 2 - 1$ or $2x = -2 - 1$ $2x = 1$ or $2x = -3$ $x = \frac{1}{2}$ or $x = -\frac{3}{2}$	✓ find root ✓ simplification ✓ answers		
		NOTE: In option 2, the simplification mark must only be awarded if the candidate states ± 2 or demonstrates it later in the solution.		(3)	
	1.1.2	$4x^2 - 11 = -12x$ $4x^2 + 12x - 11 = 0$ $x = \frac{-12 \pm \sqrt{(12)^2 - 4(4)(-11)}}{2(4)}$ $x = -3,74$ or $x = 0,74$	✓ correct substitution ✓✓ answers		
		NOTE: Penalise 1 mark for rounding in this question only. Candidate must show the substitution to obtain full marks.		(3)	
	1.1.3	$15x - 4 < 9x^2$ $\therefore -9x^2 + 15x - 4 < 0$ $\therefore 9x^2 - 15x + 4 > 0$ $(3x-1)(3x-4) > 0$ $\therefore x < \frac{1}{3}$ or $x > \frac{4}{3}$		✓ standard form ✓ factors ✓✓ answers	
		NOTE: Penalise 1 mark for use of AND instead of OR		(4)	

	<p>1.1.4 $\sqrt{2x-2} - \sqrt{7-2x} = 1$ $(\sqrt{2x-2})^2 = (\sqrt{7-2x} + 1)^2$ $2x - 2 = 7 - 2x + 2\sqrt{7-2x} + 1$ $4x - 10 = 2\sqrt{7-2x}$ $(2x - 5)^2 = (\sqrt{7-2x})^2$ $4x^2 - 20x + 25 = 7 - 2x$ $4x^2 - 18x + 18 = 0$ $\therefore 2x^2 - 9x + 9 = 0$ $(x - 3)(2x - 3) = 0$ $\therefore x = 3 \text{ or } x = \frac{3}{2}$ reject : $x \neq \frac{3}{2}$</p>	<p>✓ isolate surd and square both sides</p> <p>✓ simplification</p> <p>✓ standard form</p> <p>✓ factors</p> <p>✓ $x = 3$ and rejection</p>	(5)
1.2	<p>$a^2b^2 - 2ab - 8 = 0$ and $\log_2(a + 5) = 3$ $\log_2(a + 5) = 3$ $2^3 = a + 5$ $8 = a + 5$ $a = 3$</p> <p>$\therefore a^2b^2 - 2ab - 8 = 0$ $(3)^2b^2 - 2(3)b - 8 = 0$ $9b^2 - 6b - 8 = 0$ $(3b - 4)(3b + 2) = 0$ $b = \frac{4}{3}$ or $b = -\frac{2}{3}$</p> <p style="text-align: center;">OR</p> <p>$a^2b^2 - 2ab - 8 = 0$ and $\log_2(a + 5) = 3$ $\log_2(a + 5) = 3$ $2^3 = a + 5$ $8 = a + 5$ $a = 3$</p> <p>$a^2b^2 - 2ab - 8 = 0$ $(ab - 4)(ab + 2) = 0$ $ab = 4$ or $ab = -2$ $\therefore 3b = 4$ $3b = -2$ $b = \frac{4}{3}$ or $b = -\frac{2}{3}$</p>	<p>✓ exponential form</p> <p>✓ value of a</p> <p>✓ substitution</p> <p>✓ factors</p> <p>✓ both answers for b</p> <p style="text-align: center;">OR</p> <p>✓ exponential form</p> <p>✓ value of a</p> <p>✓ factors</p> <p>✓ substitution</p> <p>✓ both answers for b</p>	(5)

1.3	$p = \frac{\sqrt{x+2}}{\sqrt{16-x^2}}$ $\therefore x+2 \geq 0$ $\therefore x \geq -2 \dots \dots \dots (1)$ $\therefore 16-x^2 > 0$ $(4+x)(4-x) > 0$ $\therefore -4 < x < 4 \dots \dots \dots (2)$ <p>From (1) and (2)</p> $-2 \leq x < 4$	<p>✓ inequality (1)</p> <p>✓ factors ✓ inequality (2)</p> <p>✓ answer</p>	(4)
			[24]

QUESTION 2

2.1	2.1.1	$1-p; 2p-3; p+5$ $d = T_2 - T_1 = T_3 - T_2$ $\therefore (2p-3) - (1-p) = (p+5) - (2p-3)$ $2p-3-1+p = p+5-2p+3$ $3p-4 = -p+8$ $4p = 12$ $\therefore p = 3$	<p>✓ substitution</p> <p>✓ answer</p>	(2)
	2.1.2	(a) $T_1 = 1-p$ $T_1 = 1-3$ $T_1 = -2$	<p>✓ answer</p>	(1)
		(b) $T_2 = 2p-3$ $T_2 = 2(3)-3$ $\therefore T_2 = 3$ $\therefore d = T_2 - T_1$ $d = 3 - (-2)$ $d = 5$	<p>✓ answer</p>	(1)
	2.1.3	$1-p; 2p-3; p+5; \dots$ $= 1-3; 2(3)-3; 3+5; \dots$ $= -2; 3; 8; 13; 18; \dots$ <p>All the terms except T_1 end in either 3 or 8 while perfect squares end on 1; 4; 9; 6; 5; 0.</p> <p>OR</p>	<p>✓ correct terms</p> <p>✓ explanation</p>	

	T_1 is not a perfect square. OR $T_n = 5n - 7$ \therefore not a perfect square	✓✓ explanation ✓✓ $T_n = 5n - 7$	(2)
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2.2	2.2.1	$-3; -2; -3; -6; -11; \dots$ First differences: $+1; -1; -3; -5$ $T_n = a + (n-1)d$ $T_n = 1 + (n-1)(-2)$ $T_n = 1 - 2n + 2$ $T_n = -2n + 3$	✓ first differences ✓ substitution ✓ answer	(3)
	2.2.2	$T_n = -2n + 3$ $T_{35} = -2(35) + 3$ $\therefore T_{35} = -67$	✓ answer	(1)
	2.2.3	$\begin{array}{cccccc} -3 & & -2 & & -3 & & -6 & & -11 \\ & \diagdown & & \diagup & & \diagdown & & \diagup & & \diagdown \\ & 1 & & -1 & & -3 & & -5 & & \end{array}$ <p style="text-align: right;">1st differences</p> $\begin{array}{cccc} & & -2 & & -2 & & -2 \\ & & \diagdown & & \diagup & & \diagdown \\ & & & & & & \end{array}$ <p style="text-align: right;">2nd differences</p> $\begin{array}{lcl} 2a = -2 & 3a + b = 1 & a + b + c = -3 \\ a = -1 & 3(-1) + b = 1 & -1 + 4 + c = -3 \\ & b = 4 & c = -6 \end{array}$ $T_n = -n^2 + 4n - 6$ <p>OR</p> $T_n = an^2 + bn + c$ <p>but... $2a = -2$ $\therefore a = -1$ $\therefore T_n = -n^2 + bn + c$ $T_1 = -(1)^2 + b(1) + c$ $-3 = -1 + b + c$ $\therefore -2 = b + c \dots \dots (1)$ $T_2 = -(2)^2 + b(2) + c$ $-2 = -4 + 2b + c$ $\therefore 2 = 2b + c \dots \dots (2)$ $(2-1) \dots \therefore b = 4$ $sub(1) \dots -2 = 4 + c$ $\therefore c = -6$ $\therefore T_n = -n^2 + 4n - 6$</p>	✓ second differences ✓ $a = -1$ ✓ $b = 4$ ✓ $c = -6$ ✓ second differences ✓ $a = -1$ ✓ $b = 4$ ✓ $c = -6$	(4)

	2.2.4	$T_n = -n^2 + 4n - 6$ $T'(n) = -2n + 4$ $0 = -2n + 4$ $n = 2$ $\therefore T(2) = -2$ <p>\therefore NO positive terms.</p> <p>OR</p> $T_n = -n^2 + 4n - 6$ $T_n = -[n^2 - 4n + 2^2 - 4 + 6]$ $T_n = -[(n-2)^2 + 2]$ $\therefore T_n = -(n-2)^2 - 2$ $\therefore T_n(\text{max}) = -2$ <p>\therefore NO positive terms.</p> <p>OR</p> <p>Max is given as -2 and is negative</p>	<p>✓ method</p> <p>✓ $T_n(\text{max})$</p> <p>✓ method</p> <p>✓ $T_n(\text{max})$</p> <p>✓✓ Max = -2</p>	(2)
[16]				

QUESTION 3

3.1	$S_n = 4n^2 + 1$ $S_6 = 4(6)^2 + 1$ $\therefore S_6 = 145$ $S_5 = 4(5)^2 + 1$ $\therefore S_5 = 101$ $\therefore T_6 = S_6 - S_5$ $\therefore T_6 = 145 - 101$ $\therefore T_6 = 44$	<p>✓ value of S_6</p> <p>✓ value of S_5</p> <p>✓ answer</p>	(3)
3.2	$(4x-3) + (4x-3)^2 + (4x-3)^3$ $\therefore r = 4x-3$ $\therefore -1 < r < 1; \quad r \neq 0$ $-1 < 4x-3 < 1; \quad 4x-3 \neq 0$ $\therefore 2 < 4x < 4 \quad x \neq \frac{3}{4}$ $\therefore \frac{1}{2} < x < 1; \quad x \neq \frac{3}{4}$ <p>NOTE: No penalty if candidate does not state: $x \neq \frac{3}{4}$</p>	<p>✓ $r = 4x-3$</p> <p>✓ $-1 < r < 1$</p> <p>✓ answer</p>	(3)
3.3	$\sum_{k=3}^5 (-1)^k \cdot \frac{2}{k}$ $= (-1)^3 \cdot \frac{2}{3} + (-1)^4 \cdot \frac{2}{4} + (-1)^5 \cdot \frac{2}{5}$ $= -\frac{2}{3} + \frac{1}{2} - \frac{2}{5}$ $= -\frac{17}{30}$ <p>NOTE: Answer only, full marks.</p>	<p>✓ expansion</p> <p>✓ answer</p>	(2)
			[8]

QUESTION 4

4.1	$x \neq -3$	✓ answer	(1)
4.2	$y \neq 2$	✓ answer	(1)
4.3	4.3.1 6 units NOTE: Accept 6 units right, but not 6 units left.	✓ answer	(1)
	4.3.2 3,5 units NOTE: Accept 3,5 units upwards, but not 3,5 units downwards.	✓ answer	(1)
4.4	$x = -3$ $y = -\frac{3}{2}$ NOTE: Do not accept any equating in terms of p and q.	✓ answer ✓ answer	(2)
4.5	$0 = \frac{6}{x+3} - 1,5$ $\frac{3}{2} = \frac{6}{x+3}$ $3(x+3) = 6(2)$ $3x+9 = 12$ $3x = 3$ $x = 1$ (1;0) NOTE: The answer does NOT need to be given in coordinate form.	✓ answer	(1)

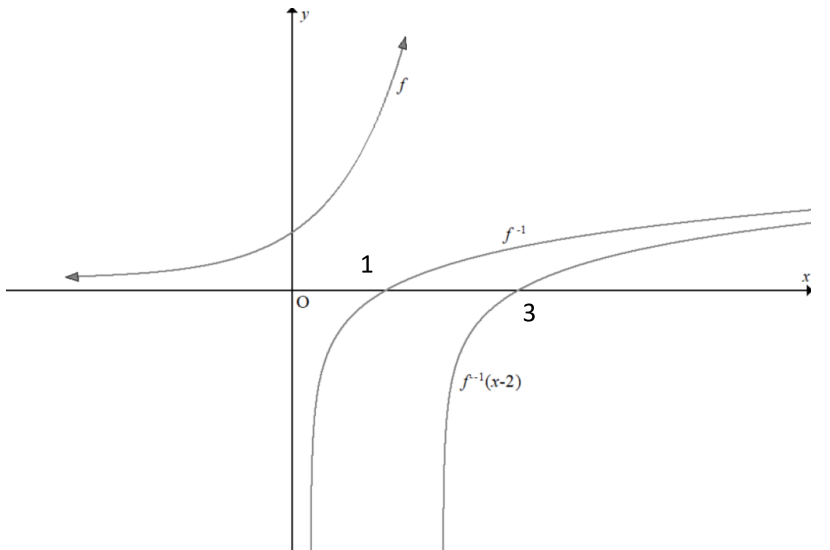
4.6		<ul style="list-style-type: none"> ✓ asymptotes ✓ intercepts ✓ shape 	(3)
4.7	$y = -x + k$ $\therefore -\frac{3}{2} = -(-3) + k$ $-\frac{3}{2} = 3 + k$ $\therefore k = -\frac{9}{2}$ <p>NOTE: Award FULL marks for Answer only</p>	<ul style="list-style-type: none"> ✓ substitute point ✓ answer 	(2)
4.8	$x > -3$	✓ answer	(1)
4.9	$y = \frac{-6}{x+3} + \frac{3}{2}$ <p>OR</p> $y = \frac{6}{-x-3} + \frac{3}{2}$ <p>OR</p> $y = -\frac{6}{x+3} + \frac{3}{2}$	✓ answer	(1)
			[14]

QUESTION 5

5.1	$E\left(\frac{7}{2}; \frac{81}{4}\right)$	✓ answer	(1)
5.2	$f(x) = -\left(x - \frac{7}{2}\right)^2 + \frac{81}{4}$ $f(1) = -\left(1 - \frac{7}{2}\right)^2 + \frac{81}{4} = 14$ $f(5) = -\left(5 - \frac{7}{2}\right)^2 + \frac{81}{4} = 18$ $\therefore AG = \frac{f(5) - f(1)}{5 - 1}$ $= \frac{18 - 14}{4}$ $\therefore AG = 1$	✓ value of $f(1)$ ✓ value of $f(5)$ ✓ substitution ✓ answer	(4)
5.3	$f(x) = -\left(x - \frac{7}{2}\right)^2 + \frac{81}{4}$ $\therefore f(x) = -x^2 + 7x + 8$ $\because f(x) = g(x)$ $\therefore -x^2 + 7x + 8 = -3x + 24$ $-x^2 + 10x - 16 = 0$ $\therefore x^2 - 10x + 16 = 0$ $(x - 2)(x - 8) = 0$ $\therefore x = 2 \text{ or } x = 8$ $\therefore x_D = 2$	✓ equating ✓ x-values ✓ answers/selection	(3)
5.4	$ST = f(x) - g(x)$ $ST = -x^2 + 7x + 8 - (-3x + 24)$ $ST = -x^2 + 7x + 8 + 3x - 24$ $ST = -x^2 + 10x - 16$	✓ method ✓ answer	(2)
5.5	For max: $\frac{d(ST)}{dx} = 0$ $\frac{d(ST)}{dx} = -2x + 10 = 0$ $2x = 10$ $\therefore x = 5$ $\text{max: } ST = -(5)^2 + 10(5) - 16$ $\therefore ST = 9$	✓ derivative = 0 ✓ value for x ✓ answer	(3)

[13]

QUESTION 6

6.1	$y = 3^x$ Inverse $x = 3^y$ $\therefore y = \log_3 x$	✓ answer	(1)
6.2	$y = f^{-1}(x) = \log_3 x$ x-intercept: $\log_3 x = 0$ $\therefore x = 3^0$ $\therefore x = 1$ y-intercept: None $y = f^{-1}(x-2) = \log_3(x-2)$ x-intercept: $\log_3(x-2) = 0$ $\therefore x-2 = 3^0$ $\therefore x = 3$ y-intercept: None 	✓ x-intercept of $f^{-1}(x) = \log_3 x$ ✓ shape $f^{-1}(x) = \log_3 x$ ✓ x-intercept of $f^{-1}(x-2) = \log_3(x-2)$ ✓ shape $f^{-1}(x-2) = \log_3(x-2)$	(4)
6.3	$\log_3(x-2) < 1$ $\therefore 2 < x < 5$	✓ critical values ✓ correct notation	(2)
			[7]

NOTE: If the candidate does not draw the graph but calculates both x-intercepts, award 2 marks. If the graph crosses the asymptote, DO NOT award the shape mark.

QUESTION 7

7.1	$A = P(1+i)^n$ $6\,000\,000 = 5\,700\,000(1+i)^7$ $\frac{6\,000\,000}{5\,700\,000} = (1+i)^7$ $\sqrt[7]{1,0526\dots} = 1+i$ $\therefore i = 1,00735 - 1$ $\therefore i = 0,00735$ <p>rate: 0,74%</p>	<p>✓ substitution into correct formula</p> <p>✓ value of i</p> <p>✓ answer</p>	(3)
7.2	<p>7.2.1</p> $P_v = \frac{x[1-(1+i)^{-n}]}{i}$ $4\,000\,000 = \frac{30\,000 \left[1 - \left(1 + \frac{0,06}{12} \right)^{-n} \right]}{\frac{0,06}{12}}$ $\frac{4\,000\,000 \times \left(\frac{0,06}{12} \right)}{30\,000} = 1 - \left(1 + \frac{0,06}{12} \right)^{-n}$ $\frac{1}{3} = \left(1 + \frac{0,06}{12} \right)^{-n}$ $\log_{\left(1 + \frac{0,06}{12} \right)} \frac{1}{3} = -n$ $n = 220,27$ <p>\therefore she will make 220 withdrawals.</p>	<p>✓ substitution into correct formula</p> <p>✓ $i = \frac{0,06}{12}$</p> <p>✓ simplification</p> <p>✓ correct use of logs</p> <p>✓ answer of 220</p>	(5)

7.2.2	$4\,000\,000 = \frac{20\,000 \left[1 - \left(1 + \frac{0,06}{12} \right)^{-n} \right]}{\frac{0,06}{12}}$ $0 = \left(1 + \frac{0,06}{12} \right)^{-n}$ <p>She can make any number (an infinite number) of withdrawals.</p> <p>Her interest earned equals her withdrawal amount. She will only be drawing the interest amount.</p> <p style="text-align: center;">OR</p> $A = P(1+i)^n$ $A = 4\,000\,000 \left(1 + \frac{0,06}{12} \right)^1$ $A = R4\,020\,000$ <p>She can make any number (an infinite number) of withdrawals.</p> <p>Her interest earned equals her withdrawal amount. She will only be drawing the interest amount.</p>	<p>✓ valid method</p> <p>✓ simplification</p> <p>✓ explanation</p> <p style="text-align: center;">OR</p> <p>✓ valid method</p> <p>✓ answer</p> <p>✓ explanation</p>	(3)
7.3	$A = P(1+i)^n$ $A = 1\,000 \left(1 + \frac{0,15}{12} \right)^{18}$ $A = R1\,250,58$ $F_v = \frac{x[(1+i)^n - 1]}{i}$ $F_v = \frac{700 \left[\left(1 + \frac{0,15}{12} \right)^{18} - 1 \right]}{\frac{0,15}{12}}$ $F_v = R14\,032,33$ $\text{Amount} = R1\,250,58 + R14\,032,33$ $\therefore \text{Amount} = R15\,282,91$	<p>✓ value of A</p> <p>✓ substitution in correct formula</p> <p>✓ value for F_v</p> <p>✓ answer</p>	(4)
[15]			

QUESTION 8

8.1	$f(x) = 3x^2 - 6$ $f(x+h) = 3(x+h)^2 - 6$ $f(x+h) = 3(x^2 + 2xh + h^2) - 6$ $f(x+h) = 3x^2 + 6xh + 3h^2 - 6$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{3x^2 + 6xh + 3h^2 - 6 - 3x^2 + 6}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{6xh + 3h^2}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{h(6x + 3h)}{h}$ $f'(x) = \lim_{h \rightarrow 0} (6x + 3h)$ $f'(x) = 6x$ <p>NOTE: Penalise 1 mark for notation error in this question only. Award ZERO marks for Answer only</p>	<p>✓ $f(x+h)$</p> <p>✓ substitution</p> <p>✓ factorisation (<i>may be implied</i>)</p> <p>✓ answer</p>	(4)
8.2	$f(x) = \left(2\sqrt{x} - \frac{1}{x}\right)^2$ $f(x) = 4x - 4 \cdot \frac{1}{\sqrt{x}} + \frac{1}{x^2}$ $f(x) = 4x - 4x^{-\frac{1}{2}} + x^{-2}$ $f'(x) = 4 + 2x^{-\frac{3}{2}} - 2x^{-3}$ <p style="text-align: center;">OR</p> $f'(x) = 4 + \frac{2}{\sqrt{x^3}} - \frac{2}{x^3}$	<p>✓ simplification</p> <p>✓ $f(x) = 4x - 4x^{-\frac{1}{2}} + x^{-2}$</p> <p>✓ 4</p> <p>✓ $2x^{-\frac{3}{2}}$ or $\frac{2}{\sqrt{x^3}}$</p> <p>✓ $-2x^{-3}$ or $\frac{2}{x^3}$</p>	(5)
8.3	$f(x) = 3x^3 - 3x^2 + 6x - 2$ $f'(x) = 9x^2 - 6x + 6$ $f''(x) = 18x - 6$ <p>for concave up</p> $18x - 6 > 0$ $\therefore x > \frac{1}{3}$ $\therefore x \in \left(\frac{1}{3}; \infty\right)$	<p>✓ $f'(x)$</p> <p>✓ $f''(x)$</p> <p>✓ correct condition of concavity</p> <p>✓ answer</p>	(4)

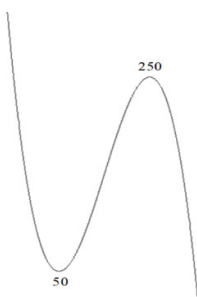
[13]

QUESTION 9

9.1	9.1.1	$f'(x) = -6x^2 - 6x + 12$ y-intercept $x = 0$ $\therefore f'(0) = 12$ $\therefore A(0 ; 12)$ NOTE: Does not have to be in coordinate form.	✓ answer	(1)
	9.1.2	x-intercepts $y = f'(x) = 0$ $-6x^2 - 6x + 12 = 0$ $\therefore x^2 + x - 2 = 0$ $(x+2)(x-1) = 0$ $\therefore x = -2 \text{ or } x = 1$ $\therefore B(-2 ; 0) \quad ; \quad C(1 ; 0)$ NOTE: Must be in coordinate form.	✓ $f'(x)$ (= 0 may be implied) ✓ factors ✓ both coordinates	(3)
	9.1.3	Turning points	✓ answer	(1)
	9.1.4	$f(x)$ increases where: $m = f'(x) > 0$ $\therefore -2 < x < 1$ OR $m = f'(x) > 0$ $\therefore x \in (-2 ; 1)$	✓ $m = f'(x) > 0$ ✓✓ answers OR ✓ $m = f'(x) > 0$ ✓✓ answers	(3)
	9.1.5	Point of inflection: $f''(x) = 0$ $\therefore -12x - 6 = 0$ $-12x = 6$ $\therefore x = -\frac{1}{2}$ $f(x) = -2x^3 - 3x^2 + 12x + 20$ $\therefore f(-\frac{1}{2}) = -2(-\frac{1}{2})^3 - 3(-\frac{1}{2})^2 + 12(-\frac{1}{2}) + 20$ $\therefore f(-\frac{1}{2}) = 13,5$	✓ $f''(x) = 0$ ✓ value for x ✓ substitution ✓ value for $f(-\frac{1}{2})$	(4)
9.2	DO NOT MARK THIS QUESTION. THIS QUESTION HAS BEEN REMOVED FROM THE EXAMINATION PAPER.			

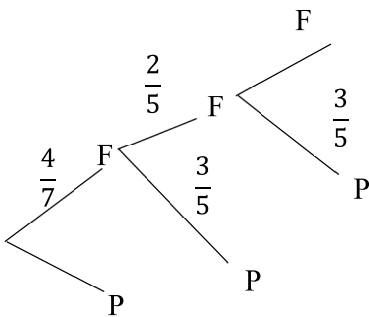
QUESTION 10

10.	$W(x) = -\frac{x^3}{150} + 3x^2 - 250x - 2700$ <p>\therefore max :</p> $W'(x) = -\frac{3x^2}{150} + 6x - 250 = 0$ $-x^2 + 300x - 12500 = 0$ $\therefore x^2 - 300x + 12500 = 0$ $(x - 250)(x - 50) = 0$ $\therefore x = 250 \text{ or } x = 50$ $W''(x) = -\frac{6x}{150} + 6$ $W''(x) = -\frac{x}{25} + 6$ $\therefore W''(50) = -\frac{50}{25} + 6 > 0$ $\therefore W''(250) = -\frac{250}{25} + 6 < 0$ <p>\therefore Maximum profit: 250 bicycles weekly.</p> <p>OR</p>	<p>✓ $W'(x)$</p> <p>✓ equate to 0</p> <p>✓ factors</p> <p>✓ values of x</p> <p>✓ $W''(x)$</p> <p>✓ $W''(50) > 0$</p> <p>✓ $W''(250) < 0$</p> <p>✓ conclusion</p>	
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$W(x) = -\frac{x^3}{150} + 3x^2 - 250x - 2700$ <p>∴ max :</p> $W'(x) = -\frac{3x^2}{150} + 6x - 250 = 0$ $-x^2 + 300x - 12500 = 0$ $\therefore x^2 - 300x + 12500 = 0$ $(x - 250)(x - 50) = 0$ $\therefore x = 250 \text{ or } x = 50$ $W(250) = -\frac{250^3}{150} + 3(250)^2 - 250(250) - 2700$ $W(250) = R18133,33$ <p>or</p> $W(50) = -\frac{50^3}{150} + 3(50)^2 - 250(50) - 2700$ $W(50) = -R8533,33$ <p>∴ Maximum profit: 250 Bicycles weekly</p> <p>OR</p> $W(x) = -\frac{x^3}{150} + 3x^2 - 250x - 2700$ <p>∴ max :</p> $W'(x) = -\frac{3x^2}{150} + 6x - 250 = 0$ $-x^2 + 300x - 12500 = 0$ $\therefore x^2 - 300x + 12500 = 0$ $(x - 250)(x - 50) = 0$ $\therefore x = 250 \text{ or } x = 50$  <p>∴ Maximum profit: 250 Bicycles weekly</p>	<ul style="list-style-type: none"> ✓ $W'(x)$ ✓ equate to 0 ✓ factors ✓ values of x ✓ substitution ✓ $W(250)$ ✓ $W(50)$ ✓ conclusion <ul style="list-style-type: none"> ✓ $W'(x)$ ✓ equate to 0 ✓ factors ✓ values of x ✓ shape ✓ min at $x = 50$ ✓ max at $x = 250$ ✓ conclusion 	
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QUESTION 11

NOTE: Candidates can present solutions either in decimal or fraction form. Do not penalise for rounding-off.

11.1	11.1.1	For independent events: $P(A) \times P(B) = P(A \text{ and } B)$ $\therefore (x + 0,1) \times (0,4) = (0,1)$ $\therefore (x + 0,1) = 0,25$ $\therefore x = 0,15$ $x + 0,1 + 0,3 + y = 1$ $0,15 + 0,1 + 0,3 + y = 1$ $\therefore y = 0,45$	✓ correct substitution ✓ value for x ✓ method ✓ value for y	(4)
	11.1.2	$0,15 + 0,3$ $= 0,45$ NOTE: Answer only, full marks.	✓ answer	(1)
11.2	 <p>F (unsuccessful)/ P (pass/succeed)</p>			
	11.2.1	$\frac{4}{7} \times \frac{3}{5} = \frac{12}{35}$ NOTE: Answer only, full marks.	✓ method ✓ answer	(2)
	11.2.2	$\frac{4}{7} \times \frac{2}{5} \times \frac{3}{5} = \frac{24}{175}$ NOTE: Answer only, full marks.	✓ method ✓ answer	(2)
[9]				

QUESTION 12

12.1	12.1.1	1 NOTE: Accept 2.	✓ answer	(1)
	12.1.2	$7! - (2! \times 6!) = 3\,600$ NOTE: Accept answer as 3 600 or $7! - (2! \times 6!)$ No CA if method is meaningless.	✓ 7! ✓ $-(2! \times 6!)$ ✓ answer	(3)
12.2	P(win) $= 0,7 \times 0,9 + 0,3 \times 0,45$ $= 0,765$ $= 76,5\%$ NOTE: No CA if method is meaningless.		method answer	(2)
				[6]
TOTAL:				145