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# Basic Education

KwaZulu-Natal Department of Education  
REPUBLIC OF SOUTH AFRICA

**MATHEMATICS P2**

**PREPARATORY EXAMINATION**

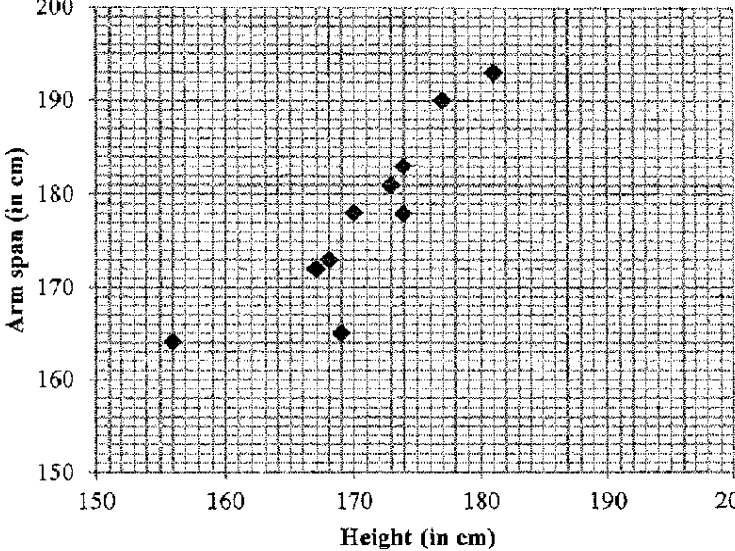
**SEPTEMBER 2015**

**MEMORANDUM**

**NATIONAL  
SENIOR CERTIFICATE**

**GRADE 12**

**QUESTION 1**

<p>1.1</p>	<p style="text-align: center;"><b>Scatter plot of Height vs Arm span</b></p> 	<p>✓ 1 – 4 points correct                  ✓ 5 – 9 points correct                  ✓ all points correct</p> <p style="text-align: right;">(3)</p>
<p>1.2</p>	<p><math>a = -36,58</math>      (<math>a = -36,57689\dots</math>)  <math>b = 1,25</math>      (<math>b = 1,25381\dots</math>)</p> <p><math>\hat{y} = -36,58 + 1,25x</math></p>	<p>✓✓ a                  ✓ b                  ✓ equation                  Eqn. only 4/4 (4)</p>
<p>1.3</p>	<p><math>\hat{y} = -36,58 + 1,25(176)</math>  <math>= 183,42</math></p> <p>OR</p> <p><math>\hat{y} = 184,09</math></p>	<p>✓ substitute 176                  ✓ answer (2)</p> <p>✓✓ answer (2)</p>
<p>1.4</p>	<p>There is strong, positive correlation between height and arm span.</p>	<p>✓ strong, positive (1)</p> <p style="text-align: right;"><b>[10]</b></p>

**QUESTION 2**

<p>2.1</p>	<table border="1"> <thead> <tr> <th>Daily Sales</th> <th>Frequency</th> <th>Cumulative Frequency</th> </tr> </thead> <tbody> <tr> <td><math>60 \leq x &lt; 70</math></td> <td>5</td> <td>5</td> </tr> <tr> <td><math>70 \leq x &lt; 80</math></td> <td>11</td> <td>16</td> </tr> <tr> <td><math>80 \leq x &lt; 90</math></td> <td>22</td> <td>38</td> </tr> <tr> <td><math>90 \leq x &lt; 100</math></td> <td>13</td> <td>51</td> </tr> <tr> <td><math>100 \leq x &lt; 110</math></td> <td>7</td> <td>58</td> </tr> <tr> <td><math>110 \leq x &lt; 120</math></td> <td>3</td> <td>61</td> </tr> </tbody> </table>	Daily Sales	Frequency	Cumulative Frequency	$60 \leq x < 70$	5	5	$70 \leq x < 80$	11	16	$80 \leq x < 90$	22	38	$90 \leq x < 100$	13	51	$100 \leq x < 110$	7	58	$110 \leq x < 120$	3	61	<p>a ✓ first two cumulative frequencies correct</p> <p>a ✓ next two cumulative frequencies correct</p> <p>a ✓ remainder correct (total = 61)</p> <p>(3)</p>
Daily Sales	Frequency	Cumulative Frequency																					
$60 \leq x < 70$	5	5																					
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$100 \leq x < 110$	7	58																					
$110 \leq x < 120$	3	61																					
<p>2.2</p>	<p style="text-align: center;"><b>Cumulative frequency graph of Daily Sales</b></p>	<p>e ca a a</p> <p>✓ grounding at 0</p> <p>✓ plotting cumulative frequencies at upper limits</p> <p>✓ points correct</p> <p>✓ smooth shape of curve</p> <p>(4)</p>																					
<p>2.3</p>	<p>The median for the data is approximately R 87. (Accept 85-89)</p>	<p>ca ✓ reading off from graph</p> <p>a ✓ R87</p> <p>(2)</p>																					
<p>2.4</p>	<p>The upper 25% interval is R96 to R120 (Range to accept: 94 to 120)</p>	<p>a ✓ 96 to 120</p> <p>(1)</p> <p>[10]</p>																					

**QUESTION 3**

<p>3.1</p>	$\frac{x_D - 1}{2} = 2 \quad \frac{y_D + 0}{2} = 2$ $x_D = 5 \quad x_D = 4$ <p>D(5 ; 4)</p>	<p>a ✓ <math>x_D = 5</math> a ✓ <math>y_D = 4</math></p> <p>(2)</p>
<p>3.2</p>	$m_{CD} = \frac{4 - (-2)}{5 - 2}$ $= 2$ <p><math>\tan \alpha = 2</math> <math>\therefore \alpha = 63,4^\circ</math></p>	<p>ca ✓ substitution into gradient formula ca ✓ <math>\tan \alpha = 2_{CD}</math> a ✓ answer</p> <p>(3)</p>
<p>3.3</p>	<p><math>m_{AB} = m_{CD} = 2</math>      AB    CD, equal gradients</p> <p><math>y = 2x + c</math> <math>0 = 2(-1) + c</math> <math>c = 2</math> <math>y = 2x + 2</math></p>	<p>ca ✓ <math>m_{AB} = 2</math> ca ✓ subst (-1 ; 0) a ✓ answer</p> <p>(3)</p>
<p>3.4</p>	$m_{AD} = \frac{4 - (0)}{5 - (-1)}$ $= \frac{2}{3}$ <p><math>\tan (\angle \text{ of inclination of AD}) = \frac{2}{3}</math> <math>\angle \text{ of inclination of AD} = 33,7^\circ</math> <math>\theta = 63,4^\circ - 33,7^\circ</math> <math>\therefore = 29,7^\circ</math></p>	<p>ca ✓ <math>m = \frac{2}{3}</math> ca on D a ✓ <math>33,7^\circ</math> ca ✓ <math>29,7^\circ</math> acute acute</p> <p>(3)</p>



**QUESTION 4**

4.1	$r^2 = (2-4)^2 + (3-5)^2$ $= 8$ $(x-2)^2 + (y-3)^2 = 8$	a ✓ subst into distance formula a ✓ 8 a ✓ $(x-2)^2$ a ✓ $(y-3)^2$ (4)
4.2	$m_{NP} = \frac{5-3}{4-2} = 1$ $m_{PT} = -1$ $y = -x + c$ $5 = -4 + c$ $c = 9$ $y = -x + 9$ $0 = -x + 9$ $x = 9$ $\therefore T(9; 0)$	a ✓ $m_{NP} = 1$ a ✓ $m_{PT} = -1$ ca ✓ subst (5; 4) a ✓ $c = 9$ ca ✓ $y = -x + 9$ a ✓ coordinates of T (6)
4.3	$PT = \sqrt{(9-4)^2 + (5-0)^2}$ $= \sqrt{50}$ $= 5\sqrt{2}$	ca ✓ substitution into distance formula a ✓ $\sqrt{50}$ (2)
4.4	$\text{Area} = \pi \times PT^2$ $= \pi \times 50$ $= 157$	ca ✓ substitution into area formula a ✓ 157 (2)
4.5	$\tan \hat{NPT} = \frac{\sqrt{8}}{\sqrt{50}}$ $\hat{NPT} = 21,8^\circ$	ca ✓ $\tan \hat{NPT} = \frac{\sqrt{8}}{\sqrt{50}}$ a ✓ $21,8^\circ$ (2)
4.6	$NP = NM$ $PT = TM$ $\therefore MNPT \text{ is a kite}$	radii radii two pairs of adjacent sides equal in length a ✓ S/R a ✓ S/R a ✓ reason (3)

<p>4.7</p>	<p> <math>\widehat{NTP} = \widehat{NTM} = 21,8^\circ</math> diagonal of kite  <math>\widehat{NPT} = \widehat{NMT} = 90^\circ</math> tangent perpendicular to radius  <math>\widehat{MNP} = 360^\circ - 90^\circ - 90^\circ - 43,6^\circ</math> angles in quadrilateral  <math>= 136,4^\circ</math>   <b>OR</b>   <math>NP \perp PT</math> (rad <math>\perp</math> tan)  <math>\therefore \widehat{TMP} = 68,2^\circ</math> (<math>\angle</math> sum <math>\Delta</math>)  <math>\widehat{TMP} = \widehat{TMN}</math> (prop of kite)  <math>\therefore \widehat{MNP} = 2(68,2^\circ)</math>  <math>\therefore \widehat{MNP} = 136,4^\circ</math> </p>	<p>ca a ca a ca a</p>	<p> <math>\checkmark</math> S/R on 45  <math>\checkmark</math> S/R  <math>\checkmark</math> S/R  <math>\checkmark</math> answer (4)   <math>\checkmark</math> S/R  <math>\checkmark</math> S/R  <math>\checkmark</math> S/R  <math>\checkmark</math> answer (4)  <b>[23]</b> </p>
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## QUESTION 5

5.1	$\frac{\tan(180^\circ + A) \cdot \cos(180^\circ - A) \cdot \sin(360^\circ - A)}{\cos(90^\circ - A)}$ $= \frac{(\tan A)(-\cos A)(-\sin A)}{\sin A}$ $= \frac{\sin A}{\cos A} \cdot \cos A$ $= \sin A$	<p>a ✓ <math>\tan A</math> ✓ <math>-\cos A</math>  a ✓ <math>-\sin A</math> ✓ <math>\sin A</math>  a ✓ <math>\frac{\sin A}{\cos A}</math>  ca ✓ answer <i>assign</i></p> <p>(6)</p>
5.2.1	$\cos 52^\circ = \cos 2(26^\circ)$ $= 2\cos^2 26^\circ - 1$ $= 2(r)^2 - 1$ $= 2r^2 - 1$	<p>a ✓ writing <math>52^\circ</math> in terms of <math>26^\circ</math>  a ✓ expansion  a ✓ answer</p> <p>(3)</p>
5.2.2	$\tan 71^\circ = \frac{\sin 71^\circ}{\cos 71^\circ}$ $= \frac{\sin(45^\circ + 26^\circ)}{\cos(45^\circ + 26^\circ)}$ $= \frac{\sin 45^\circ \cos 26^\circ + \cos 45^\circ \sin 26^\circ}{\cos 45^\circ \cos 26^\circ - \sin 45^\circ \sin 26^\circ}$ $= \frac{\left(\frac{\sqrt{2}}{2}\right)r + \left(\frac{\sqrt{2}}{2}\right)(\sqrt{1-r^2})}{\left(\frac{\sqrt{2}}{2}\right)r - \left(\frac{\sqrt{2}}{2}\right)(\sqrt{1-r^2})}$ $= \frac{\left(\frac{\sqrt{2}}{2}\right)(r + \sqrt{1-r^2})}{\left(\frac{\sqrt{2}}{2}\right)(r - \sqrt{1-r^2})}$ $= \frac{r + \sqrt{1-r^2}}{r - \sqrt{1-r^2}}$	<p>a ✓ identity  a ✓ writing in terms of <math>26^\circ</math>  a ✓ expansions  a ✓ <math>\sqrt{1-r^2}</math>  ca ✓ substitution</p> <p>a ✓ answer</p> <p>(6)</p>

5.3	$LHS = \frac{\sin 2x}{\cos 2x + \sin^2 x}$ $= \frac{2 \sin x \cos x}{\cos^2 x - \sin^2 x + \sin^2 x}$ $= \frac{2 \sin x \cos x}{\cos^2 x}$ $= \frac{2 \sin x}{\cos x}$ $= 2 \tan x$ $= RHS$	<p>a ✓ identity for sin2x</p> <p>a ✓ identity for cos 2x</p> <p>a ✓ simplification</p> <p>a ✓ identity</p> <p style="text-align: right;">(4)</p>
	<p><b>OR</b></p> $LHS = \frac{\sin 2x}{\cos 2x + \sin^2 x}$ $= \frac{2 \sin x \cos x}{2 \cos^2 x - 1 + \sin^2 x}$ $= \frac{2 \sin x \cos x}{2 \cos^2 x - (1 - \sin^2 x)}$ $= \frac{2 \sin x \cos x}{2 \cos^2 x - \cos^2 x}$ $= \frac{2 \sin x \cos x}{\cos^2 x}$ $= \frac{2 \sin x}{\cos x}$ $= 2 \tan x$ $= RHS$	<p>a ✓ identity for sin2x</p> <p>a ✓ identity for cos 2x</p> <p>a ✓ simplification</p> <p>a ✓ identity</p> <p style="text-align: right;">(4)</p>
	<p><b>OR</b></p> $LHS = \frac{\sin 2x}{\cos 2x + \sin^2 x}$ $= \frac{2 \sin x \cos x}{1 - 2 \sin^2 x + \sin^2 x}$ $= \frac{2 \sin x \cos x}{1 - \sin^2 x}$ $= \frac{2 \sin x \cos x}{\cos^2 x}$ $= \frac{2 \sin x}{\cos x}$ $= 2 \tan x$ $= RHS$	<p>a ✓ identity for sin2x</p> <p>a ✓ identity for cos 2x</p> <p>a ✓ simplification</p> <p>a ✓ identity</p> <p style="text-align: right;">(4)</p>

[19]

**QUESTION 6**

<p>6.1</p>	$\cos 2x = \sin(x - 30^\circ)$ $= \cos[90^\circ - (x - 30^\circ)]$ $= \cos(120^\circ - x)$ <p>key angle = <math>120^\circ - x</math></p> $2x = 120^\circ - x + n.360^\circ; n \in Z$ $3x = 120^\circ + n.360^\circ; n \in Z$ $x = 40^\circ + n.120^\circ; n \in Z$ <p>or</p> $2x = 360^\circ - (120^\circ - x) + n.360^\circ; n \in Z$ $2x = 240^\circ + x + n.360^\circ; n \in Z$ $x = 240^\circ + n.360^\circ; n \in Z$	<p>a ✓ using co-ratio</p> <p>a ✓ <math>120^\circ - x</math></p> <p>a ✓ <math>2x = 120^\circ - x + n.360^\circ</math></p> <p>ca ✓ <math>x = 40^\circ + n.120^\circ</math></p> <p>ca ✓ <math>-2x = 360^\circ - (120^\circ - x) + n.360^\circ</math></p> <p>a ✓ <math>x = 240^\circ + n.360^\circ</math></p> <p>a ✓ <math>n \in Z</math></p> <p>(7)</p>
<p>6.2</p>		<p>f</p> <p>a ✓ x-intercepts</p> <p>a ✓ turning points</p> <p>a ✓ shape and pts</p> <p>g</p> <p>a ✓ intercepts</p> <p>a ✓ turning points</p> <p>a ✓ shape</p> <p>(6)</p>
<p>6.3</p>	$-120^\circ < x < -80^\circ \text{ or } 40^\circ < x \leq 90^\circ$	<p>a ✓ critical values: <math>-120^\circ; -80^\circ</math></p> <p>a ✓ critical values: <math>40^\circ; 90^\circ</math></p> <p>ca ✓ correct notation</p> <p>(3)</p>

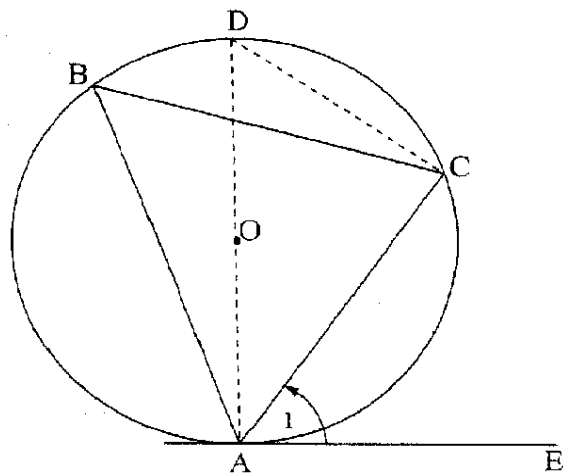
[16]

**QUESTION 7**

7.1	$\tan x = \frac{AB}{BD}$ $= \frac{h}{BD}$ $BD = \frac{h}{\tan x}$	<p>a ✓ using tan ratio</p> <p>a ✓ <math>BD = \frac{h}{\tan x}</math></p> <p>(2)</p>
7.2	$BC = BD$ $CD^2 = BC^2 + BD^2 - 2BC \cdot BD \cdot \cos y$ $= \left(\frac{h}{\tan x}\right)^2 + \left(\frac{h}{\tan x}\right)^2 - 2\left(\frac{h}{\tan x}\right)\left(\frac{h}{\tan x}\right) \cdot \cos y$ $= \frac{h^2}{\tan^2 x} + \frac{h^2}{\tan^2 x} - \frac{2h^2}{\tan^2 x} \cdot \cos y$ $= \frac{2h^2}{\tan^2 x} - \frac{2h^2}{\tan^2 x} \cdot \cos y$ $= \frac{2h^2}{\tan^2 x} (1 - \cos y)$ $= \frac{2h^2 (1 - \cos y)}{\tan^2 x}$	<p>a ✓ using cosine formula</p> <p>ca ✓ substitution 7.1.</p> <p>a ✓ simplification</p> <p>a ✓ common factor</p> <p>(4)</p> <p>[6]</p>

**QUESTION 8**

8.1



Construction: Draw diameter AD. Join D to C

Proof:

$$\hat{EAC} + \hat{DAC} = 90^\circ$$

tan  $\perp$  radius

$$\hat{DCA} = 90^\circ$$

$\angle$  in semi circle

$$\hat{ADC} + \hat{DAC} = 90^\circ$$

sum of  $\angle$ s in  $\Delta$

$$\therefore \hat{EAC} = \hat{ADC}$$

$$\text{But } \hat{ABC} = \hat{ADC}$$

$\angle$ s in the same segment

$$\therefore \hat{EAC} = \hat{ABC}$$

$\checkmark$  construction

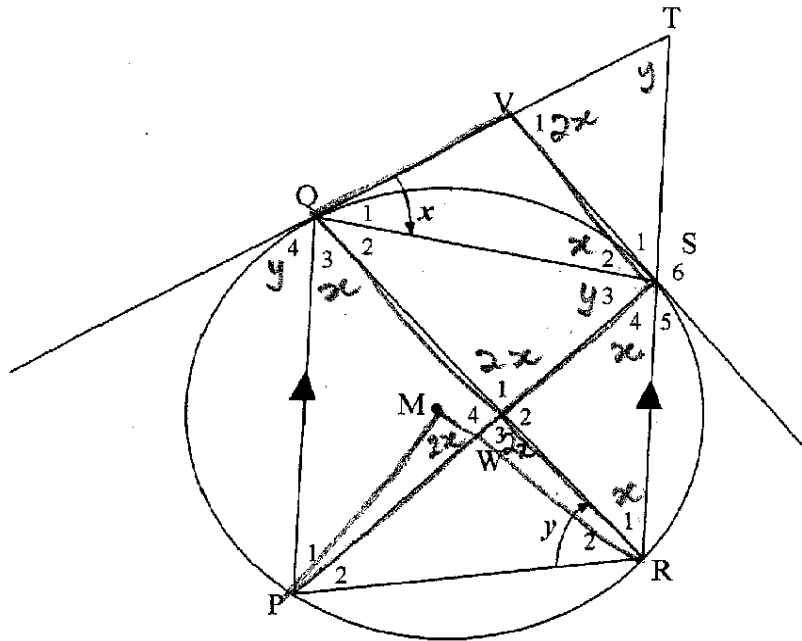
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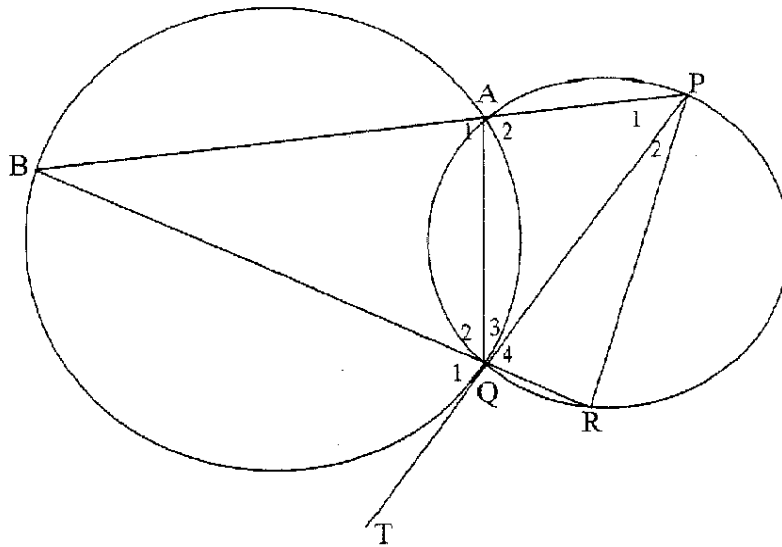
$\checkmark$  S  $\checkmark$  R

(6)



8.2.1	Two tangents drawn from the same external point are equal in length.	$a$	✓ answer	(1)
8.2.2 (a)	$\hat{S}_2 = x$	angles opposite equal sides	$a$	✓ S ✓ R (2)
8.2.2 (b)	$\hat{R}_1 = x$	tan-chord theorem	$a$	✓ S ✓ R (2)
8.2.2 (c)	$\hat{V}_1 = 2x$	ext $\angle$ of $\Delta$	$a$	✓ S ✓ R (2)
8.2.3	$\hat{R}_1 = \hat{Q}_3 = x$ $\hat{Q}_3 = \hat{S}_4 = x$ $\therefore \hat{R}_1 = \hat{S}_4$	alt $\angle$ s; $PQ \parallel RS$ $\angle$ s in the same segment chord PR	$a$	✓ S ✓ R ✓ S ✓ R (4)
8.2.4	$\hat{W}_1 = 2x$ $\hat{W}_1 = \hat{V}_1$ $\therefore QVSW$ is a cyclic quad	ext $\angle$ of $\Delta$ converse: ext $\angle$ of cyclic quad	$a$	✓ S ✓ R ↑ ✓ S ✓ R (4)
8.2.5 (a)	$\hat{Q}_4 = y$	tan-chord theorem	$a$	✓ S ✓ R (2)
8.2.5 (b)	$\hat{T} = \hat{Q}_4 = y$	corresp $\angle$ s; $PQ \parallel RS$ OR ext $\angle$ of $\Delta$	$a$	✓ S ✓ R (2)
8.2.6	Join M to R and M to P $\hat{Q}_3 = x$ $\hat{P}M\hat{R} = 2x$ $\hat{P}M\hat{R} = \hat{W}_3 = 2x$ $\therefore PMWR$ is a cyclic quad	proven in 8.2.3 $\angle$ at centre = $2 \times \angle$ at circumference converse: angles in same segment	$a$	✓ S / R ✓ S ✓ R (3) [28]

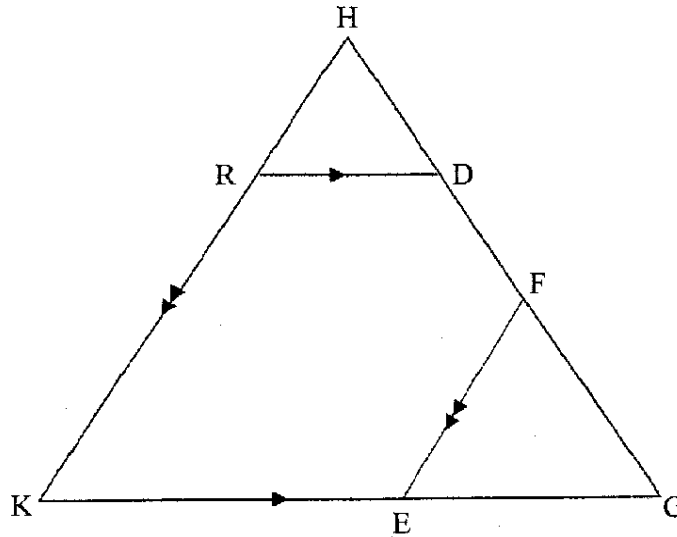
**QUESTION 9**



<p>9.1</p>	$\hat{Q}_4 = \hat{Q}_1$ $\hat{Q}_1 = \hat{A}_1$ $\hat{A}_1 = \hat{R}$ $\Rightarrow \hat{Q}_4 = \hat{R}$ $\therefore PQ = PR$	vert opp angles tan-chord theorem ext angle of cyclic quad  sides opp equal angles	a a a  a ✓ S ✓ R ✓ S ✓ R ✓ S ✓ R  ✓ R	(7)
<p>9.2</p>	In $\triangle PBQ$ and $\triangle PQA$ (i) $\hat{P}_1$ is common (ii) $\hat{B} = \hat{Q}_3$ (iii) $\hat{PQB} = \hat{A}_2$ $\therefore \triangle PBQ \parallel \triangle PQA$	tan-chord theorem remaining angles in triangle equiangular	a a a } } } ✓ S ✓ S ✓ R ✓ S / R	(4)
<p>9.3</p>	$\frac{PA}{PQ} = \frac{PQ}{PB}$ But $PQ = PR$ $\therefore \frac{PA}{PR} = \frac{PR}{PB}$ $\therefore PA, PR$ and $PB$ form a geometric sequence	from 9.2   the ratio is constant	a  a  a ✓ deduction ✓ $PQ = PR$  ✓ conclusion in full	(3)

[14]

**QUESTION 10**



<p>10.1</p>	<p>In <math>\Delta HKG</math>:  <math>\frac{DG}{HD} = \frac{RK}{RH}</math>  <math>\frac{DG}{2} = \frac{9}{3}</math>  <math>\therefore DG = 6</math></p> <p>(prop theorem; <math>RD \parallel KG</math>)</p>	<p>a ✓ S / R                  a ✓ substitution                  a ✓ answer                  (3)</p>
<p>10.2</p> <p><del>DG-FD</del></p>	<p>Let <math>FD = y</math>  <math>\therefore FG = 6 - y</math>  <math>\frac{GF}{FH} = \frac{GE}{EK}</math>  <math>\frac{6-y}{y+2} = \frac{1}{2}</math>  <math>2(6-y) = y + 2</math>  <math>12 - 2y = y + 2</math>  <math>-3y = -10</math>  <math>\therefore y = \frac{10}{3} = FD</math></p> <p>(prop theorem; <math>FE \parallel HK</math>)</p>	<p>Ca ✓ statement <del>DG-FD</del>                  a ✓ S / R                  Ca ✓ substitution                  a ✓ simplification                  a ✓ answer                  (5)                  [8]</p>

**TOTAL: 150**