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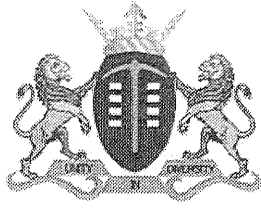
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# **PREPARATORY EXAMINATION**

**2015**

## **MEMORANDUM**

**SUBJECT: MATHEMATICS P2/ WISKUNDE V2 (10612)**

GAUTENG DEPARTMENT OF EDUCATION  
PREPARATORY EXAMINATION – 2015

MATHEMATICS/WISKUNDE  
(Second Paper/Tweede Vraestel)

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MEMORANDUM

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**NOTE:**

- If a candidate answered a QUESTION TWICE, mark the FIRST attempt ONLY.
- Consistent accuracy applies in ALL aspects of the memorandum.
- Penalise for rounding **only** in QUESTION 3.6
- Assuming answers/values in order to solve a problem is NOT ACCEPTABLE.
- S/R refers to STATEMENT as well as REASON

**NOTA:**

- *As 'n kandidaat 'n vraag TWEEKEER beantwoord, merk slegs die EERSTE poging.*
- *Volgehoue akkuraatheid word in ALLE aspekte van die nasienmemorandum toegepas.*
- *Penalisering vir afronding word slegs in vraag 3.6 toegepas.*
- *Aanvaarding van antwoorde/waardes om 'n probleem op te los, is ONAANVAARBAAR.*
- *S/R verwys na BEWERING sowel as die REDE.*

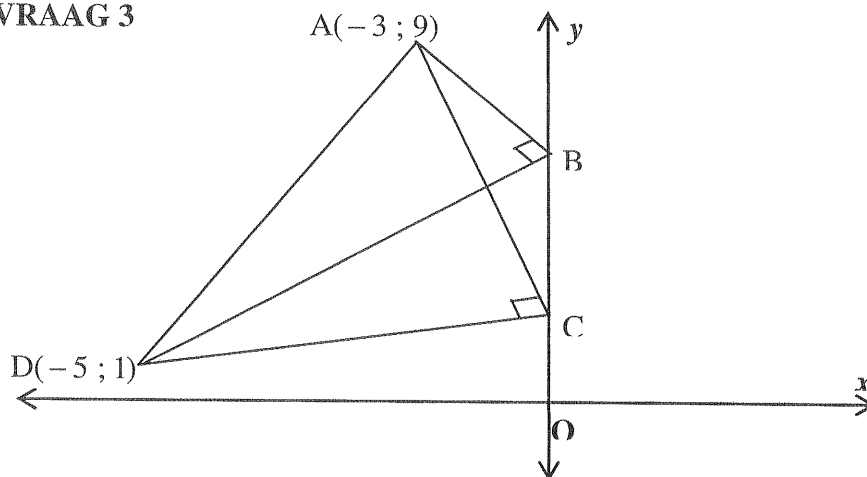
## QUESTION / VRAAG 1

1.1		<p>✓ <math>(\bar{x}; \bar{y})</math> (22,6 ; 44,5)</p> <p>✓ line of best fit <i>beste paslyn/lyn van beste passing</i></p> <p style="text-align: right;">(2)</p>
1.2.1	25 years /25 jaar	✓ answer / <i>antwoord</i> (1)
1.2.2	<p>The reaction time according to the line of best fit for age 25 should be 51,46. The reaction time of this patient is <math>\pm 65</math>.</p> <p><i>Die reaksietyd volgens die lyn van beste passing vir die ouderdom van 25 moet 51,46 wees. Die reaksietyd vir hierdie pasiënt is <math>\pm 65</math>.</i></p>	<p>✓ answer / <i>antwoord</i> (1)</p> <p><b>Any other valid explanation.</b> <b><i>Enige ander geldige verduideliking</i></b></p>
1.3	<p>A = -21,03 B = 2,90</p> <p><math>y = 2,90x - 21,03</math></p>	<p>✓ A = -21,03 ✓ B = 2,90</p> <p>✓ <math>y = 2,90x - 21,03</math></p> <p style="text-align: right;">(3)</p>
1.4	<p><math>r = 0,95</math></p> <p>very strong correlation / <i>baie sterk korrelasie</i></p>	<p>✓ <math>r = 0,95</math> ✓ very strong / strong <i>baie sterk / sterk</i></p> <p style="text-align: right;">(2)</p>
1.5	<p>The 30 year olds have a higher reaction time on average. The interquartile range of this group is bigger (IQR = 15) than that of the 15 year olds (IQR=5). The reaction time of the 30 year olds varies more.</p> <p><i>Die 30-jariges het gemiddeld 'n hoër reaksietyd. Die interkwartielvariasiewydte van hierdie groep is groter (IQR=15). as dié van die 15-jariges (IQR=5).. Die reaksietyd van die 30-jariges varieer meer.</i></p>	<p>✓ IOR ✓ for comments / <i>vir kommentaar</i></p> <p style="text-align: right;">(2) <b>[11]</b></p>

## QUESTION / VRAAG 2

2.1	<table border="1"> <thead> <tr> <th>Age in years <i>Ouderdom in jare</i></th> <th>Number of people <i>Aantal mense</i></th> <th>Cumulative frequency <i>Kumulatiewe frekwensie</i></th> </tr> </thead> <tbody> <tr> <td><math>0 \leq A &lt; 10</math></td> <td>20</td> <td>20</td> </tr> <tr> <td><math>10 \leq A &lt; 20</math></td> <td>130</td> <td>150</td> </tr> <tr> <td><math>20 \leq A &lt; 30</math></td> <td>152</td> <td>302</td> </tr> <tr> <td><math>30 \leq A &lt; 40</math></td> <td>92</td> <td>394</td> </tr> <tr> <td><math>40 \leq A &lt; 60</math></td> <td>86</td> <td>480</td> </tr> <tr> <td><math>60 \leq A &lt; 80</math></td> <td>18</td> <td>498</td> </tr> <tr> <td><math>80 \leq A &lt; 100</math></td> <td>2</td> <td>500</td> </tr> </tbody> </table>	Age in years <i>Ouderdom in jare</i>	Number of people <i>Aantal mense</i>	Cumulative frequency <i>Kumulatiewe frekwensie</i>	$0 \leq A < 10$	20	20	$10 \leq A < 20$	130	150	$20 \leq A < 30$	152	302	$30 \leq A < 40$	92	394	$40 \leq A < 60$	86	480	$60 \leq A < 80$	18	498	$80 \leq A < 100$	2	500	<p>✓ all answers/ <i>alle antwoorde</i></p> <p>(1)</p>
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$80 \leq A < 100$	2	500																								
2.2		<p>✓ plotting of points <i>plot van punte</i></p> <p>✓ joining of points <i>verbind van punte</i></p> <p>✓ grounding point at (0 ; 0) <i>grond punt by (0 ; 0)</i></p> <p>(3)</p>																								
2.3.1	<p>26 years old (accept 25 – 27) <i>26 jaar oud (aanvaar 25-27)</i></p>	<p>✓ answer <i>antwoord</i></p> <p>(1)</p>																								
2.3.2	<p><math>\frac{90}{500} \times 100</math> <math>= 18\%</math>    The percentage of people 16 and above 18 is 82%</p> <p><i>Die persentasie mense 16 jaar en ouer is 82%</i></p>	<p>✓ 90</p> <p>✓ 18%</p> <p>✓ 82%</p> <p>(3)</p> <p>[8]</p>																								

## QUESTION / VRAAG 3



3.1	$M\left(\frac{-3-5}{2}; \frac{9+1}{2}\right)$ $M(-4; 5)$	$\checkmark x = -4$ $\checkmark y = 5$	(2)
3.2	$AM^2 = (-4+3)^2 + (5-9)^2$ $= 1 + 16$ $= 17$ $\therefore r = \sqrt{17}$ <p><b>OR/OF</b></p> $AD^2 = (-5+3)^2 + (1-9)^2$ $= 4 + 64$ $= 68$ $\therefore AD = \sqrt{68}$ $\therefore \text{radius} = \frac{\sqrt{68}}{2}$ $= \sqrt{17}$	$\checkmark$ correct substitution into distance formula <i>korrekte vervanging in afstand formule</i> $\checkmark r = \sqrt{17}$  $\checkmark$ correct substitution into distance formula <i>korrekte vervanging in afstand formule</i>  $\checkmark r = \sqrt{17}$	(2)
3.3	<p>Yes, the circle will pass through point C</p> <p><i>Ja, die sirkel gaan deur punt C</i></p> <p><math>\hat{B} = \hat{C} = 90^\circ</math>, AD is the diameter line subtends equal <math>\angle^s</math>.</p> <p><math>\hat{B} = \hat{C} = 90^\circ</math>, AD die middellyn lynstuk onderspan gelyke <math>\angle^e</math></p>	$\checkmark$ yes / ja  $\checkmark$ reason / rede	(2)

3.4	<p>B(0 ; y)</p> $m_{AB} \times m_{BD} = -1$ $\left(\frac{9-y}{-3-0}\right)\left(\frac{1-y}{-5-0}\right) = -1$ $(9-y)(1-y) = -15$ $9 - 10y + y^2 = -15$ $y^2 - 10y + 24 = 0$ $(y-6)(y-4) = 0$ <p style="text-align: center;"><math>\therefore y = 6</math> or <math>y = 4 \quad \therefore B(0;6)</math></p> <p><b>OR/OF</b></p> $AB^2 + BD^2 = AD^2$ $(9-y)^2 + (-3-0)^2 + (-5-0)^2 + (1-y)^2 = (-5+3)^2 + (1-9)^2$ $81 - 18y + y^2 + 9 + 25 + 1 - 2y + y^2 = 4 + 64$ $2y^2 - 20y + 48 = 0$ $y^2 - 10y + 24 = 0$ $(y-6)(y-4) = 0$ <p style="text-align: center;"><math>y = 6</math> or <math>y = 4</math> <math>\therefore B(0;6)</math></p>	<p><math>\checkmark m_{AB} \times m_{BD} = -1</math></p> <p><math>\checkmark \left(\frac{9-y}{-3-0}\right) / \left(\frac{1-y}{-5-0}\right)</math></p> <p><math>\checkmark</math> standard form <i>standaardvorm</i></p> <p><math>\checkmark</math> factors / faktore</p> <p><math>\checkmark B(0 ; 6)</math></p> <p style="text-align: right;">(5)</p> <p><math>\checkmark (9-y)^2 + (-3-0)^2 + (-5-0)^2 + (1-y)^2 = (-5+3)^2 + (1-9)^2</math></p> <p><math>\checkmark (-5+3)^2 + (1-9)^2</math></p> <p><math>\checkmark</math> standard form/ <i>Standaardvorm</i></p> <p><math>\checkmark</math> factors / faktore</p> <p><math>\checkmark B(0 ; 6)</math></p> <p style="text-align: right;">(5)</p>
3.5	$m_{AB} = \frac{9-6}{-3-0}$ $= -1$ $m_{\parallel} = -1$ <p><math>y - y_1 = m(x - x_1)</math>      <b>OR/OF</b>    <math>y = -x + c</math></p> <p><math>y - 1 = -1(x + 5)</math>                      <math>-5 = -1 + c</math></p> <p><math>y - 1 = -x - 5</math>                            <math>c = -4</math></p> <p><math>y = -x - 4</math>                                <math>y = -x - 4</math></p>	<p><math>\checkmark m_{\parallel} = -1</math></p> <p><math>\checkmark</math> substitution of <math>(-1 ; 5)</math> <i>vervangings van <math>(-1 ; 5)</math></i></p> <p><math>\checkmark y = -x - 4</math></p> <p style="text-align: right;">(3)</p>

3.6	$m_{AD} = \frac{1-9}{-5+3} = 4$ $\tan \theta = 4$ $\theta = 76^\circ$ $m_{DB} = \frac{1-6}{-5-0} = 1$ $\tan \alpha = 1$ $\alpha = 45^\circ$ $\hat{BDA} = 76^\circ - 45^\circ = 31^\circ$ <p style="text-align: center;">ext <math>\angle</math> of <math>\Delta</math></p> <p><b>OR/OF</b></p> $AB^2 = (-3-0)^2 + (9-6)^2$ $AB = \sqrt{18}$ $BD^2 = (-5-0)^2 + (1-6)^2$ $BD = \sqrt{50}$ $\tan \hat{BDA} = \frac{\sqrt{18}}{\sqrt{50}} = 0,6$ $\hat{BDA} = 31^\circ$	$\checkmark m_{AD} = \frac{1-9}{-5+3} = 4$ $\checkmark \tan \theta = 4$ $\checkmark 76^\circ$ $\checkmark \tan \alpha = 1$ $\checkmark 45^\circ$ $\checkmark 31^\circ \text{ (-1 if NOT rounded)}$ $31^\circ \text{ (-1 as NIE afgerond)}$ $\checkmark (-3-0)^2 + (9-6)^2$ $\checkmark AB = \sqrt{18}$ $\checkmark (-5-0)^2 + (1-6)^2$ $\checkmark BD = \sqrt{50}$ $\checkmark \text{using a correct trig ratio}$ $\text{gebruik korrekte trig verh}$ $\checkmark 31^\circ \text{ (-1 if NOT rounded)}$ $31^\circ \text{ (-1 as NIE afgerond)}$ <p style="text-align: right;">(6) [20]</p>
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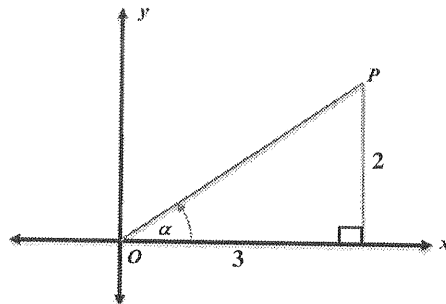
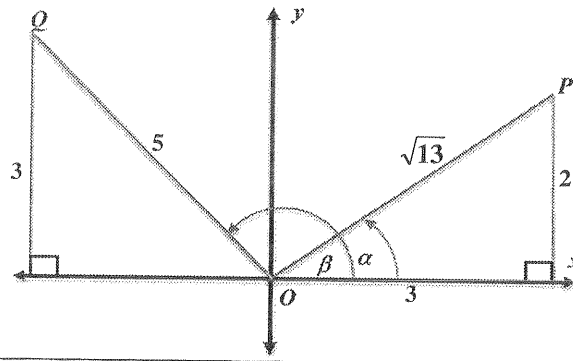
## QUESTION / VRAAG 4

4.1.1	$x^2 + y^2 - 2x + 6y = 0$ $(x-1)^2 - 1 + (y+3)^2 - 9 = 0$ $(x-1)^2 + (y+3)^2 = 1+9$ $(x-1)^2 + (y+3)^2 = 10$ $\therefore \text{centre : } (1; -3)$ $\therefore \text{radius : } \sqrt{10}$	$\checkmark (x-1)^2 - 1$ $\checkmark (y+3)^2 - 9$ $\checkmark (1; -3)$ $\checkmark \sqrt{10}$ <p style="text-align: right;">(4)</p>
4.1.2	$m_{\text{radius}} = \frac{-3+4}{1+2} = \frac{1}{3}$ $\therefore m_r \times m_t = -1$ $\therefore m_t = -3$ <p>equation of tangent / vergelyking van raaklyn</p> $y+4 = -3(x+2) \quad \text{OR} \quad y = -3x + c$ $y+4 = -3x-6 \quad -4 = -3(-2) + c$ $y = -3x-10 \quad \therefore c = -10$ $y = -3x-10$	$\checkmark m_r = \frac{1}{3}$ $\checkmark m_t = -3$ $\checkmark \text{substitution of } (-2; -4)$ $\text{vervanging van } (-2; -4)$ $\checkmark y = -3x-10$ <p style="text-align: right;">(4)</p>



	<p style="text-align: center;"> <math>B(-1; 6)</math>  <math>A(2; 3)</math>  <math>R(p; q)</math>  <math>2x + 5y + 1 = 0</math> </p>	
4.2.1	$RA = RB$ $RA^2 = RB^2$ $(p-2)^2 + (q-3)^2 = (p+1)^2 + (q-6)^2$ $p^2 - 4p + 4 + q^2 - 6q + 9 = p^2 + 2p + 1 + q^2 - 12q + 36$ $-6p + 6q = 24$ $\therefore p - q = -4$	$\checkmark RA^2 = RB^2$ $\checkmark (p-2)^2 + (q-3)^2$ $\checkmark (p+1)^2 + (q-6)^2$ $\checkmark -6p + 6q = 24$ <p style="text-align: right;">(4)</p>
4.2.2	<p style="text-align: center;"><math>R(p; q)</math> lies on the line / lê op dielyn</p> $2x + 5y + 1 = 0$ $2p + 5q = -1 \dots\dots(1)$ $p - q = -4$ $p = q - 4 \dots\dots(2)$ OR sub(1) into (2) / verv (1) in (2) $2p - 2q = -8 \dots\dots(2)$ $2p - 2q = -8 \dots\dots(2)$ $2(q-4) + 5q = -1$ $2p + 5q = -1 \dots\dots(1)$ $2q - 8 + 5q = -1$ (2) - (1) $7q = 7$ $7q = 7$ $q = 1$ $q = 1$ sub q into equation (2) / verv q in vgl (2) $p = 1 - 4$ $p = -3$ $R(-3; 1)$ radius = RA      OR/OF      radius = RB $RA^2 = (-3-2)^2 + (1-3)^2$ $RB^2 = (-3+1)^2 + (1-6)^2$ $= 25 + 4$ $= 4 + 25$ $RA = \sqrt{29}$ $RB = \sqrt{29}$ $(x+3)^2 + (y-1)^2 = 29$	$\checkmark 2p + 5q = -1$  $\checkmark 2(q-4) + 5q = -1 /$ $2p - 2q = -8$  $\checkmark q = 1$  $\checkmark p = -3$  $\checkmark RA^2 / RB^2$  $\checkmark RA / RB = \sqrt{29}$ $\checkmark (x+3)^2 + (y-1)^2 = 29$ <p style="text-align: right;">(7) [19]</p>

## QUESTION / VRAAG 5

5.1.1	$3y - 2x = 0$ $3y = 2x$ $y = \frac{2}{3}x$ $\tan \alpha = m$ $\tan \alpha = \frac{2}{3}$	$\checkmark y = \frac{2}{3}x$ $\checkmark \tan \alpha = m$ <p style="text-align: right;">(2)</p>
5.1.2	 $OP^2 = 2^2 + 3^2 \quad \text{Pyth}$ $OP = \sqrt{13}$ $\sin \alpha = \frac{2}{\sqrt{13}} \quad \text{or/of} \quad \frac{2\sqrt{13}}{13} \quad (\text{with rational denominator})$ <p style="text-align: center;">(met rasionale noemer)</p>	$\checkmark OP = \sqrt{13}$ $\checkmark \sin \alpha = \frac{2}{\sqrt{13}}$ <p style="text-align: right;">(2)</p>
5.2.1	 $\widehat{QOP} = \beta - \alpha$	$\checkmark \beta - \alpha$ <p style="text-align: right;">(1)</p>
5.2.2	$\sin \widehat{QOP} = \sin(\beta - \alpha)$ $= \sin \beta \cos \alpha - \cos \beta \sin \alpha$ $= \left( \frac{3}{5} \times \frac{3}{\sqrt{13}} \right) - \left( \frac{-4}{5} \times \frac{2}{\sqrt{13}} \right)$ $= \frac{17}{5\sqrt{13}}$	$\checkmark \sin(\beta - \alpha)$ $= \sin \beta \cos \alpha - \cos \beta \sin \alpha$ $\checkmark \frac{3}{5} \times \frac{3}{\sqrt{13}}$ $\checkmark \frac{-4}{5} \times \frac{2}{\sqrt{13}}$ $\checkmark \frac{17}{5\sqrt{13}}$ <p style="text-align: right;">(4) [9]</p>

## QUESTION / VRAAG 6

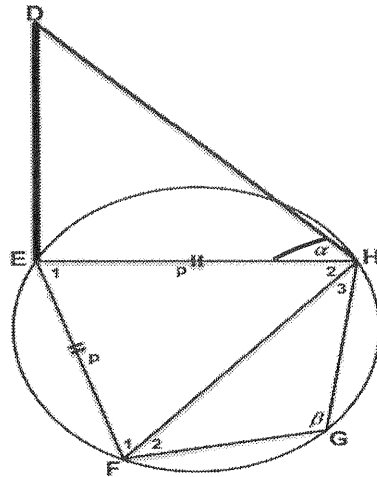
6.1	$\frac{\cos(40^\circ - x) \cdot \cos x - \sin(40^\circ - x) \cdot \sin x}{\sin 205^\circ \cdot \cos 25^\circ}$ $= \frac{\cos(40^\circ - x + x)}{-\sin 25^\circ \cdot \cos 25^\circ}$ $= \frac{\cos(40^\circ - x + x)}{-\frac{1}{2}(2 \sin 25^\circ \cdot \cos 25^\circ)}$ $= \frac{\cos 40^\circ}{-\frac{1}{2} \sin 50^\circ}$ $= \frac{\cos 40^\circ}{-\frac{1}{2} \cos 40^\circ} \quad \text{OR/OF} \quad \frac{\sin 50^\circ}{-\frac{1}{2} \sin 50^\circ}$ $= -2$	$\checkmark \cos(40^\circ - x + x)$ $\checkmark -\sin 25^\circ$ $\checkmark -\frac{1}{2} \sin 50^\circ$ $\checkmark \sin 50^\circ = \cos 40^\circ \text{ or/of}$ $\cos 40^\circ = \sin 50^\circ \text{ in numerator}$ $\text{in noemer}$ $\checkmark -2$ <p style="text-align: right;">(5)</p>
6.2.1	$\text{LHS/LK} = \frac{\cos^2 x - \sin^2 x}{\cos x + \sin x}$ $= \frac{(\cos x - \sin x)(\cos x + \sin x)}{\cos x + \sin x}$ $= \cos x - \sin x$ $= \text{RHS/RK}$	$\checkmark \cos 2x = \cos^2 x - \sin^2 x$ $\checkmark \text{factorising /faktorisering}$ <p style="text-align: right;">(2)</p>
6.2.2	$\cos x \left( \frac{\cos 2x}{\cos x + \sin x} \right) = \frac{1}{2}$ $\cos x (\cos x - \sin x) = \frac{1}{2}$ $\cos^2 x - \cos x \sin x = \frac{1}{2}$ $2 \cos^2 x - 2 \cos x \sin x = 1$ $2 \cos^2 x - 1 = 2 \cos x \sin x$ $\cos 2x = \sin 2x$	$\checkmark \cos x - \sin x$ $\checkmark \cos^2 x - \cos x \sin x = \frac{1}{2}$ $\checkmark 2 \cos^2 x - 1 = \cos 2x$ $\checkmark 2 \cos x \sin x = \sin 2x$ <p style="text-align: right;">(4)</p>
6.2.3	$\cos x \left( \frac{\cos 2x}{\cos x + \sin x} \right) = \frac{1}{2}$ $\cos 2x = \sin 2x$ $\tan 2x = 1$ $2x = 45^\circ + k \cdot 180^\circ \quad ; \quad k \in \mathbb{Z}$ $x = 22,5^\circ + k \cdot 90^\circ \quad ; \quad k \in \mathbb{Z}$ <p><b>OR/OF</b></p>	$\checkmark \tan 2x = 1$ $\checkmark 2x = 45^\circ + k \cdot 180^\circ$ $\checkmark x = 22,5^\circ + k \cdot 90^\circ \quad ; \quad k \in \mathbb{Z}$ <p style="text-align: right;">(3)</p>

	$\cos 2x = \sin 2x$ $\cos 2x = \cos(90^\circ - 2x)$ $2x = 90^\circ - 2x + k.360^\circ$ or $2x = 2x - 90^\circ + k.360^\circ$ ; $k \in Z$ $4x = 90^\circ + k.360^\circ$ ; $k \in Z$ $x = 22,5^\circ + k.90^\circ$ ; $k \in Z$	$\checkmark \cos 2x = \cos(90^\circ - 2x)$  $\checkmark 4x = 90^\circ + k.360^\circ$ $\checkmark x = 22,5^\circ + k.90^\circ$	(3)
6.3.1	Area $\Delta ABC = \frac{1}{2}mn \sin 4x$	$\checkmark$ Area $\Delta ABC = \frac{1}{2}mn \sin 4x$	(2)
6.3.2	Max area if $\sin 4x = 1$ $4x = 90^\circ$ $x = 22,5^\circ$	$\checkmark \sin 4x = 1$ $\checkmark x = 22,5^\circ$	(2)
6.3.3	Right-angled triangle/ <i>Reghoekige driehoek</i>	$\checkmark$ answer	
			[18]

## QUESTION / VRAAG 7

7.1	$\sin(60^\circ - \theta) = 1$ $60^\circ - \theta = 90^\circ$ $\theta = -30^\circ$	$\checkmark \theta = -30^\circ$	(1)
7.2	period / periode = $\frac{360^\circ}{2}$ $= 180^\circ$	$\checkmark 180^\circ$	(1)
7.3	$-2 \leq y \leq 0$ of / or $[-2; 0]$	$\checkmark -2 \leq y \leq 0$	(1)
7.4	$45^\circ < x < 135^\circ$ or/or $150^\circ < x \leq 180^\circ$	$\checkmark 45^\circ$ and $135^\circ$ $\checkmark 150^\circ$ and $180^\circ$ $\checkmark$ ALL inequalities correct <i>ALLE ongelykhede korrek</i> <b>Subtract 1 mark for extra intervals</b> <b>Trek 1 punt af vir ekstra intervalle</b>	(3)
7.5	$90^\circ < x < 150^\circ$	$\checkmark 90^\circ$ and/en $150^\circ$ $\checkmark$ inequalities / <i>ongelykhede</i>	(2)
			[8]

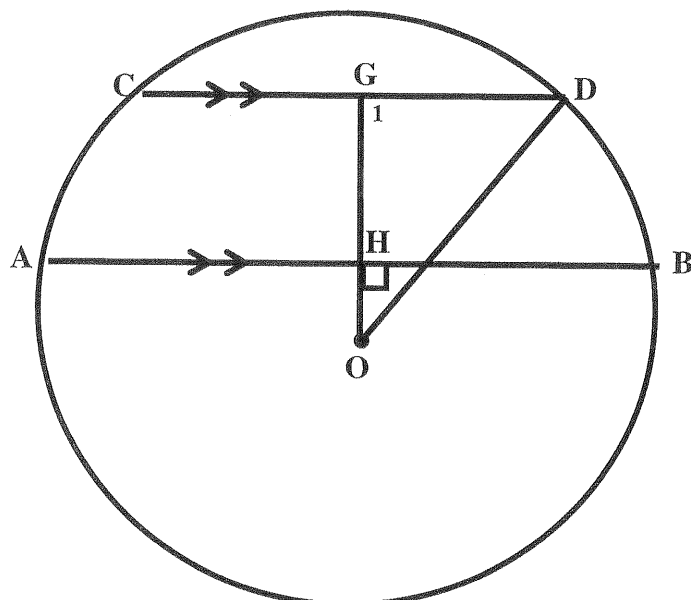
## QUESTION / VRAAG 8



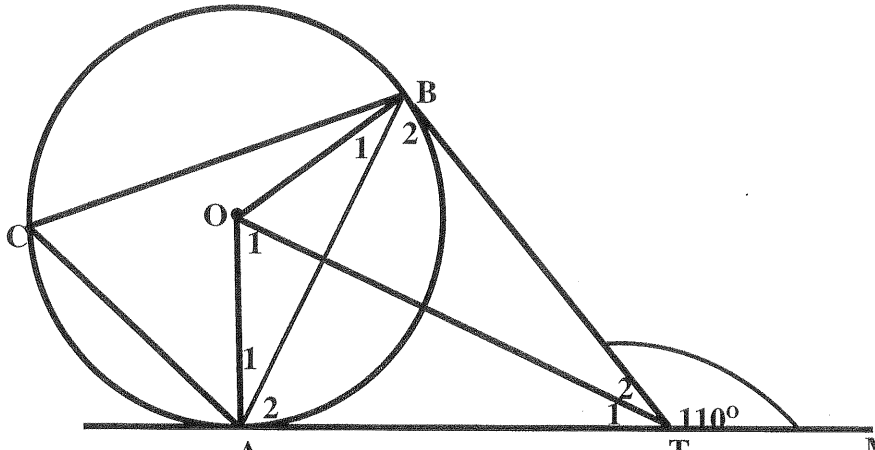
8.1	$\frac{DE}{p} = \tan \alpha$ $DE = p \tan \alpha$	$\checkmark p \tan \alpha \quad (1)$
8.2.1	$\hat{E}_1 = 180^\circ - \beta \quad (\text{opp } \angle^s \text{ of cyclic quad teenoorst. } \angle^e \text{ van kvh})$ $\hat{F}_1 = \hat{H}_2 \quad (\angle^s \text{ opp equal sides; } EH = EF \angle^e \text{ teenoor gelyke sye})$ $\hat{F}_1 + \hat{H}_2 = 180^\circ - (180^\circ - \beta) \quad (\angle^s \text{ of } \Delta / \angle^e \text{ van } \Delta)$ $= \beta$ $\hat{F}_1 = \hat{H}_2 = \frac{1}{2} \beta$	$\checkmark \hat{E}_1 = 180^\circ - \beta \text{ with reason/met rede}$ $\checkmark \hat{F}_1 = \hat{H}_2 \text{ with reason/met rede}$ $\checkmark \hat{F}_1 + \hat{H}_2 = \beta \quad (3)$
8.2.2	<p>In <math>\triangle EFH</math></p> $\frac{p}{\sin \frac{1}{2} \beta} = \frac{FH}{\sin(180^\circ - \beta)}$ $p = \frac{FH \cdot \sin \frac{1}{2} \beta}{\sin \beta}$ $= \frac{FH \cdot \sin \frac{1}{2} \beta}{2 \sin \frac{1}{2} \beta \cdot \cos \frac{1}{2} \beta}$ $= \frac{FH}{2 \cos \frac{1}{2} \beta}$	$\checkmark \text{substitution in sine rule}$ $\text{vervang in sinus formule}$ $\checkmark p = \frac{FH \cdot \sin \frac{1}{2} \beta}{\sin \beta}$ $\checkmark \sin \beta = 2 \sin \frac{1}{2} \beta \cdot \cos \frac{1}{2} \beta \quad (3)$
8.2.3	$FH^2 = p^2 + p^2 - 2p^2 \cos(180^\circ - \beta)$ $= 2p^2 + 2p^2 \cos \beta$ $= 2p^2(1 + \cos \beta)$ $FH = p\sqrt{2(1 + \cos \beta)}$	$\checkmark \text{substitution in cosine rule}$ $\text{vervang in kosinus reël}$ $\checkmark 2p^2 + 2p^2 \cos \beta$ $\checkmark 2p^2(1 + \cos \beta) \quad (3)$

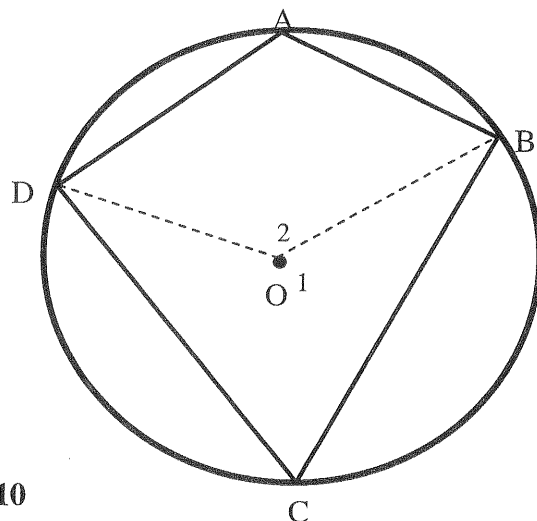
[10]

## QUESTION / VRAAG 9



S/R	Statement and reason	S/R	Bewering en rede
9.1.1	(a) $AB \parallel CD$ corr. $\angle^s$ equal / ooreenk $\angle^c$ gelyk (b) line from centre $\perp$ to chord / Midpt. $O$ ; Midpt. koord (c) Radius		<p>✓ reason / rede</p> <p>✓ reason / rede</p> <p>✓ reason / rede</p>
9.1.2	<p>Join <math>OB</math> / Verbind <math>OB</math></p> <p><math>HB = 12</math> and/en <math>GD = 5</math> (line from centre <math>\perp</math> to chord / Midpt. <math>O</math> ; Midpt. koord)</p> <p>In <math>\triangle OHB</math></p> $(OH)^2 = (OB)^2 - (BH)^2 \quad \hat{H} = 90^\circ \text{ (Pyth)}$ $= (13)^2 - (12)^2$ $= 25$ <p><math>OH = 5</math></p> <p>In <math>\triangle OGD</math></p> $(OG)^2 = (OD)^2 - (GD)^2$ $= (13)^2 - (5)^2$ $= 144$ <p><math>OG = 12</math></p> <p><math>GH = OG - OH</math></p> $= 12 - 5$ $= 7$		<p>✓ S/R</p> <p>✓ Pythagoras</p> <p>✓ <math>OH = 5</math></p> <p>✓ <math>OG = 12</math></p> <p>✓ <math>GH = 7</math></p>

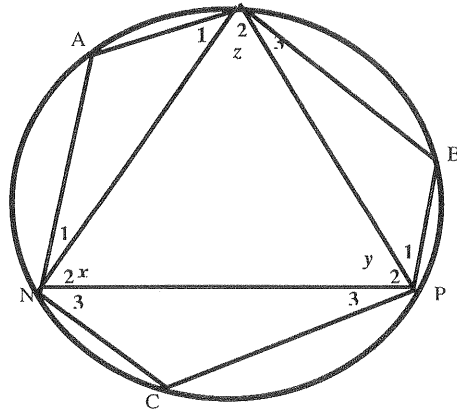
9.2.1	<p>Tangents from same point / Tans from common pt  <i>Raaklyne vanuit dies. punt</i></p> 	<p>✓ reason /rede  (1)</p>
9.2.1	<p><math>\hat{B}_1 + \hat{B}_2 = 90^\circ</math> (tan <math>\perp</math> rad / raaklyn <math>\perp</math> radius)  <math>\hat{A}_1 + \hat{A}_2 = 90^\circ</math> (tan <math>\perp</math> rad / raaklyn <math>\perp</math> radius)  <math>\therefore</math> AOBT is a cyclic quadrilateral/is 'n koordevierhoek  <i>(opposite <math>\angle</math>'s supplementary/oorstaande <math>\angle</math>'e suppl)</i></p>	<p>✓ S/R    ✓ S/R    ✓ R  (3)</p>
9.2.2	<p>OA = OB (radii)  <math>\hat{T}_1 = \hat{T}_2</math> (equal chords subtend equal angles/  <i>gelyke hoeke onderspan deur gelyke koorde</i>)</p>	<p>✓ OA = OB  (radii)  ✓ R  (2)</p>
9.2.3	<p><math>\hat{A}_2 + \hat{B}_2 = 110^\circ</math> (ext <math>\angle</math> of <math>\Delta</math> / buite <math>\angle</math> van <math>\Delta</math>)  But <math>\hat{A}_2 = \hat{B}_2</math> (<math>\angle</math>'s opp equal sides / <math>\angle</math>'e teenoor gelyke sye)  <math>\hat{A}_2 = 55^\circ</math> or <math>\hat{B}_2 = 55^\circ</math>  <math>\hat{A}_2 = \hat{B}_2 = \hat{C} = 55^\circ</math> (tan chord / <math>\angle</math> tussen raaklyn en koord)</p> <p><b>OR/OF</b></p> <p><math>\hat{O}_1 + \hat{O}_2 = 110^\circ</math> (ext <math>\angle</math> of cycl quad/buite <math>\angle</math> van kvh)  <math>\hat{O}_1 + \hat{O}_2 = 2\hat{C}</math> (<math>\angle</math> at centre = <math>2 \times \angle</math> at circ /midpts <math>\angle = 2 \times</math> omtreks <math>\angle</math>)  <math>\hat{C} = 55^\circ</math></p>	<p>✓ S/R  ✓ S/R  ✓ <math>\hat{C} = 55^\circ</math>  ✓ S/R  (4)</p> <p>✓ S/R  ✓ S  ✓ R  ✓ <math>\hat{C} = 55^\circ</math>  (4)  [17]</p>



## QUESTION / VRAAG 10

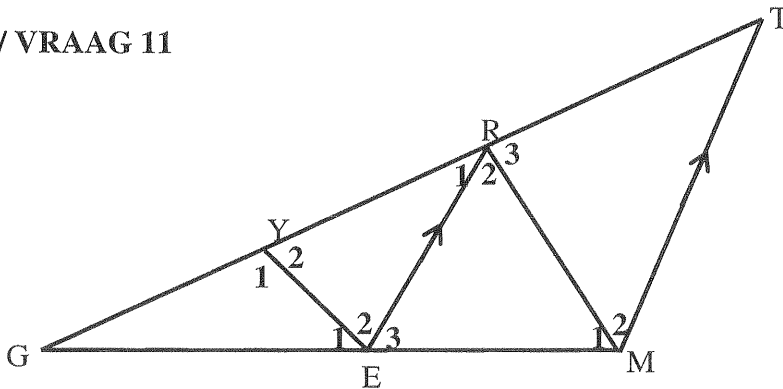
10.1	<p>Construction: Join OD and OB  <i>Konstruksie: Verbind OD en OB</i></p> <p><math>\hat{O}_1 = 2\hat{A}</math> (<math>\angle</math> at centre = <math>2 \times \angle</math> at circumference /  Midpts <math>\angle = 2 \times</math> Omtreks <math>\angle</math>)</p> <p><math>\hat{O}_2 = 2\hat{C}</math> (<math>\angle</math> at centre = <math>2 \times \angle</math> at circumference /  Midpts <math>\angle = 2 \times</math> Omtreks <math>\angle</math>)</p> <p><math>\hat{O}_1 + \hat{O}_2 = 360^\circ</math> (<math>\angle</math>'s round a pt OR <math>\angle</math>'s in a rev  <math>\angle</math>'s om 'n punt OF omwenteling</p> <p><math>2\hat{A} + 2\hat{C} = 360^\circ</math>  <math>2(\hat{A} + \hat{C}) = 360^\circ</math>  <math>\hat{A} + \hat{C} = 180^\circ</math></p> <p style="text-align: center;">M</p>	<p>✓ Construction / Konstruksie</p> <p>✓ S/R</p> <p>✓ S/R</p> <p>✓ S/R</p> <p>✓ <math>2\hat{A} + 2\hat{C} = 360^\circ</math></p> <p style="text-align: right;">(5)</p>
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10.2.1	$\hat{A} = 180^\circ - y$ $\hat{B} = 180^\circ - x$ (opp $\angle^s$ of cyclic quad / $\hat{C} = 180^\circ - z$ teenoorst. $\angle^e$ van kvh )	✓ all 3 statements al 3 bewerings ✓ reason rede (2)
10.2.2	$(180^\circ - y) + (180^\circ - x) + (180^\circ - z)$ $= 540^\circ - (x + y + z)$ $= 540^\circ - 180^\circ$ (sum of $\angle^s$ of $\Delta = 180^\circ$ ) $= 360^\circ$	✓ substitution of angles vervanging van hoeke ✓ simplification vereenvoudiging ✓ $180^\circ$ ✓ answer / antw (4) <b>[11]</b>

QUESTION / VRAAG 11



11.1	$\hat{R}_2 = \hat{M}_2$ (alt $\angle^s$ RE $\parallel$ TM / verw. $\angle^e$ ; RE $\parallel$ TM) $\hat{R}_1 = \hat{T}$ corr $\angle^s$ RE $\parallel$ TM / ooreenk. $\angle^e$ RE $\parallel$ TM)	✓ (S) ✓ (R) ✓ (S) ✓ (R) (4)
11.2	$\frac{EM}{EG} = \frac{RT}{RG}$ (line $\parallel$ one side of $\Delta$ OR prop theorem; RE $\parallel$ TM) (lyn $\parallel$ een sy van $\Delta$ ) But / Maar RT = RM ( $\angle^s$ opp equal sides ; $\hat{M}_2 = \hat{T}$ / $\angle^e$ teenoor gelyke sye ; $\hat{M}_2 = \hat{T}$ ) $\frac{EM}{EG} = \frac{RM}{RG}$	✓ (S) ✓ (R) ✓ (S) ✓ (R) (4)

11.3	<p>In <math>\triangle GYE</math> en <math>\triangle GER</math></p> <p><math>\hat{G} = \hat{G}</math> (common /gemeenskaplik)</p> <p><math>\hat{E}_1 = \hat{R}_1</math> (given /gegee)</p> <p><math>\hat{Y}_1 = \hat{E}_1 + \hat{E}_2</math> (3rd <math>\angle</math> of <math>\triangle</math> / 3e <math>\angle</math> van <math>\triangle</math>)</p> <p><math>\triangle GYE \parallel \triangle GER</math> (<math>\angle, \angle, \angle</math>)</p>	<p>✓ <math>\hat{G} = \hat{G}</math> (S/R)</p> <p>✓ <math>\hat{E}_1 = \hat{R}_1</math> (S/R)</p> <p>✓ <math>\hat{Y}_1 = \hat{E}_1 + \hat{E}_2</math> (S/R)</p> <p>✓ equiangular <math>\triangle</math> /gelykhoekige <math>\triangle</math> or/of <math>\angle, \angle, \angle</math> (R)</p> <p>(4)</p>
11.4	<p><math>\frac{EG}{EY} = \frac{RG}{RE} = \frac{YG}{EG}</math> (equiang <math>\triangle</math>'s / <math>\triangle GYE \parallel \triangle GER</math>)</p> <p><math>\therefore \frac{EG}{EY} = \frac{RG}{RE}</math></p>	<p>✓ (R) equiang <math>\triangle</math>'s / <math>\triangle GYE \parallel \triangle GER</math> gelyk <math>\triangle</math>'s <math>\triangle GYE \parallel \triangle GER</math></p> <p>(1)</p>
11.5.1	<p><math>(RG)^2 = (GM)^2 - (RM)^2</math> <math>\hat{G}\hat{R}\hat{M} = 90^\circ</math> Pythag.</p> <p><math>= (10)^2 - (6)^2</math></p> <p><math>= 64</math></p> <p><math>\therefore RG = 8</math></p>	<p>✓ substitute into Pyth <i>vervang in Pyth</i></p> <p>✓ <math>RG = 8</math></p> <p>(2)</p>
11.5.2	<p><math>\frac{GE}{GM} = \frac{GR}{GT}</math> (line <math>\parallel</math> one side of <math>\triangle</math> OR prop theorem; RE <math>\parallel</math> TM (lyn <math>\parallel</math> een sy van <math>\triangle</math>))</p> <p><math>\frac{GE}{10} = \frac{8}{14}</math></p> <p><math>GE = 5\frac{5}{7}</math> or/of <math>\frac{40}{7}</math> or/of 5,71 units/eenhede</p>	<p>✓ <math>\frac{GE}{GM} = \frac{GR}{GT}</math> /reason / rede</p> <p>✓ <math>GT = 14</math></p> <p>✓ substitution of values <i>vervang van waardes</i></p> <p>✓ answer /antwoord</p> <p>(4) [19]</p>

TOTAL/TOTAAL: 150

